

GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER– III (OLD) EXAMINATION – SUMMER 2022****Subject Code:130002****Date:08-07-2022****Subject Name:Advanced Engineering Mathematics****Time:02:30 PM TO 05:30 PM****Total Marks:70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

MARKS

- Q.1** (a) (i) Define Dirac – Delta function. **02**
(ii) Find the inverse laplace transform of in $\frac{s^2+1}{(s+1)(s-2)^2}$ **05**
(b) Find the series solution of $y''=2y'$ in powers of x. **07**

- Q.2** (a) (i) Find the fourier sine series of $f(x) = e^x$ in $0 < x < \pi$. **03**
(ii) $\frac{dy}{dx} + 2y \tan x = \sin x$ **04**
(b) Find the Fourier series of $f(x) = x + |x|$ in the interval $-\pi < x < \pi$. **07**

OR

- (b) Find the Fourier series for **07**

$$f(x) = -\pi; \quad \pi < x < 0$$

$$f(x) = -\pi; \quad \pi < x < 0$$

$$= x - \pi; \quad 0 < x < \pi$$

- Q.3** (a) (i) Find the value of $B(\frac{3}{2}, \frac{1}{2})$. **02**
(ii) Show that $\int_0^\infty \frac{\lambda^3 \sin \lambda x}{\lambda^4 + 4} d\lambda = \frac{\pi}{2} e^{-x} \cos x$, where $x > 0$. **05**
(b) Solve $y'' + a^2 y = \tan x$ by using Variation of Parameters. **07**

OR

- Q.3** (a) (i) $ye^x dx + (2y + e^x) dy = 0$. **03**
(ii) $y''' - 3y'' + 3y' - y = 4e^t$ **04**
(b) Using the power- series method, **07**
Solve $(1 - x^2)y'' - 2xy' + 2y = 0$

- Q.4** (a) (i) Find the Laplace transform of $\frac{e^{-t} \sin t}{t}$. **03**
(ii) Find the inverse Laplace transform of $\log(1 + \frac{w^2}{s^2})$. **04**
(b) Using the convolution method to solve $\frac{s+2}{(s^2+4s+5)^2}$ **07**

OR

- Q.4 (a)** (i) Solve $y''' - 6y' + 11y' - 6y = 0$. **03**
(ii) $x^2y'' - xy' + y = \sin(\log x)$ **04**
(b) Solve $y'' + 4y' + 3y = e^{-t}$, $y(0) = y'(0) = 1$. **07**

- Q.5 (a)** (i) Solve $(y + z)p + (z + x)q = x + y$ **03**
(ii) $x^2ydx - (x^3 + xy^2)dy = 0$. **04**
(b) Solve $\frac{\partial u}{\partial x} = 2\frac{\partial u}{\partial t} + u$, where $u(x, 0) = 6e^{-3x}$ by method of separation variables. **07**

OR

- Q.5 (a)** (i) Form a Partial Differential Equation by eliminating the arbitrary constants from the equation $z = (x - 2)^2 + (y - 3)^2$ **03**
(ii) Solve $(D^2 - 2DD' + D'^2)z = e^x + 2y + x^3$ **04**
(b) Solve $y'' + 2y' + 4y = 2x^2 + 3e^{-x}$ by using method of Undetermined coefficients. **07**
