

GUJARAT TECHNOLOGICAL UNIVERSITY

BE- SEMESTER-VII EXAMINATION – WINTER 2025

Subject Code:3171003

Date:15-11-2025

Subject Name:Digital Signal Processing

Time:10:30 AM TO 01:00 PM

Total Marks:70

Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

| | MARKS |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|
| Q.1 (a) Define the following systems: Moving Average, Compressor, Accumulator. | 03 |
| (b) Determine Z.T for the sequence $x(n) = -a^n u(-n-1)$ and discuss its ROC. | 04 |
| (c) Define linear convolution and obtain the same for two infinite duration sequences given as, $x_1(n) = a^n u(n)$ & $x_2(n) = b^n u(n)$. | 07 |
| Q.2 (a) State and prove time reversal property of Z.T. | 03 |
| (b) A stable LTI system is represented by the difference equation $y(n) - x(n) + \frac{1}{5}x(n-1) - \frac{1}{7}y(n-1) = 0$, find its impulse response using DTFT. | 04 |
| (c) Determine the original sequence $x(n)$ if its Z.T is given by $X(z) = \frac{1+2z^{-1}+z^{-2}}{1-\frac{3}{2}z^{-1}+\frac{1}{2}z^{-2}}$, $ Z > 1$. | 07 |
| OR | |
| (c) Determine zero input response of a system represented by a LCCDE $y(n) - 3y(n-1) - 4y(n-2) = 0$, if its solution is exponential with initial conditions $y(-1) = 5$ & $y(-2) = 0$. | 07 |
| Q.3 (a) If a system is having a difference equation $x(n) + 0.9y(n-1) - y(n) = 0$, then find (i) its Inverse System (ii) Impulse response of the Inverse System. | 03 |
| (b) Realize the following FIR system function $H(z) = 1 + \frac{1}{2}z^{-1} + \frac{3}{4}z^{-2} + \frac{1}{2}z^{-3} + z^{-4}$ with minimum numbers of multipliers. | 04 |
| (c) Define All pass system and obtain minimum phase-all pass decomposition for the system with $H(z) = \frac{(1+3z^{-1})(1-0.5z^{-1})}{z^{-1}(1+0.3z^{-1})}$ | 07 |

OR

| | |
|-----------------------------------------------------------------------------------------------------------------------------------|-----------|
| Q.3 (a) A causal system function is $H(z) = \frac{1-z^{-1}}{(1+0.75z^{-1})}$, then obtain corresponding impulse response. | 03 |
| (b) Explain types of linear phase FIR Systems. | 04 |
| (c) Explain All pass system in detail with derivation of magnitude, phase, group delay and its applications. | 07 |

- Q.4** (a) Compare FIR and IIR filters. **03**
 (b) Compute 4 point DFT of a sequence **04**
 $x[n] = \delta[n] - 2\delta[n-1] + 3\delta[n-2] + 2\delta[n-3]$.
 (c) If $H(z) = 8 * \frac{1-0.5z^{-1}+1.375z^{-2}-0.25z^{-3}}{1-1.25z^{-1}+0.75z^{-2}-0.125z^{-3}}$, then obtain direct form-I and II realizations. **07**
- OR**
- Q.4** (a) Give advantages and disadvantages of digital filters. **03**
 (b) Compute IDFT of $X(k) = (4, 2, 0, 4)$. **04**
 (c) Discuss structures for Linear phase FIR Systems. **07**
- Q.5** (a) Explain frequency warping and Pre-warping regarding filter design. **03**
 (b) Discuss Kaiser Window for FIR Filter design. **04**
 (c) Explain signal flow graph of the decimation in frequency decomposition of an N point DFT computation into two N/2 point computation if N=8. **07**
- OR**
- Q.5** (a) Discuss symmetry property of DFT. **03**
 (b) Explain Goertzel Algorithm. **04**
 (c) Enlist methods for IIR filter design and explain any one in detail. **07**
