

Subject Name & Code:

BASIC ELECTRICAL ENGINEERING- BE01R00051

Assignment – 2

Q-1: An alternating voltage is given by $v=325\sin(314t)$ Determine: (a) Peak value (b) RMS value (c) Frequency (d) Time period

Answer:

Given:

$$V_m = 325 \text{ V}, \omega = 314 \text{ rad/s}$$

To Find:

(a) Peak value, (b) RMS value, (c) Frequency, (d) Time period

Formulas:

$$V_{\text{rms}} = \frac{V_m}{\sqrt{2}}, f = \frac{\omega}{2\pi}, T = \frac{1}{f}$$

Solution:

(a) Peak value = 325 V

(b) $V_{\text{rms}} = \frac{325}{\sqrt{2}} = 229.8 \text{ V}$

(c) $f = \frac{314}{2\pi} = 50 \text{ Hz}$

(d) $T = \frac{1}{50} = 0.02 \text{ s}$

Final Answer:

$$V_m = 325 \text{ V}, V_{\text{rms}} = 229.8 \text{ V}, f = 50 \text{ Hz}, T = 0.02 \text{ s}$$

Q-2: A sinusoidal current has peak value of 15 A. Find: (a) RMS value (b) Average value (c) Form factor (d) Peak factor

Answer:

Given: $I_m = 15 \text{ A}$

(a) RMS value:

$$I_{\text{rms}} = \frac{I_m}{\sqrt{2}} = \frac{15}{\sqrt{2}} \approx 10.61 \text{ A}$$

(b) Average value (full cycle):

$$I_{avg} = \frac{2I_m}{\pi} = \frac{30}{\pi} \approx 9.55 \text{ A}$$

(c) Form factor:

$$FF = \frac{I_{rms}}{I_{avg}} = \frac{10.61}{9.55} \approx 1.111$$

(d) Peak factor:

$$PF = \frac{I_m}{I_{rms}} = \sqrt{2} \approx 1.414$$

Final Answer:

$$I_{rms} = 10.61 \text{ A}, I_{avg} = 9.55 \text{ A}, FF = 1.111, PF = 1.414$$

Q-3: Two voltages are given as: $V_1=100\angle 0^\circ\text{V}$ and $V_2=80\angle 30^\circ\text{V}$. Find the resultant voltage using phasor method.

Answer:

Given:

$$V_1 = 100\angle 0^\circ = 100 + j0$$

$$V_2 = 80\angle 30^\circ = 80(\cos 30^\circ + j\sin 30^\circ) = 69.282 + j40$$

To Find: Resultant voltage $V_R = V_1 + V_2$

Formula:

Phasor addition:

$$V_R = (a_1 + a_2) + j(b_1 + b_2)$$

$$\text{Magnitude: } |V_R| = \sqrt{(\text{Re})^2 + (\text{Im})^2}$$

$$\text{Angle: } \theta = \tan^{-1}\left(\frac{\text{Im}}{\text{Re}}\right)$$

Solution:

$$\text{Re} = 100 + 69.282 = 169.282$$

$$\text{Im} = 0 + 40 = 40$$

$$|V_R| = \sqrt{(169.282)^2 + (40)^2} = \sqrt{28656.4 + 1600} = \sqrt{30256.4} = 173.98 \text{ V}$$

$$\theta = \tan^{-1}\left(\frac{40}{169.282}\right) = \tan^{-1}(0.2363) = 13.3^\circ$$

Final Answer:

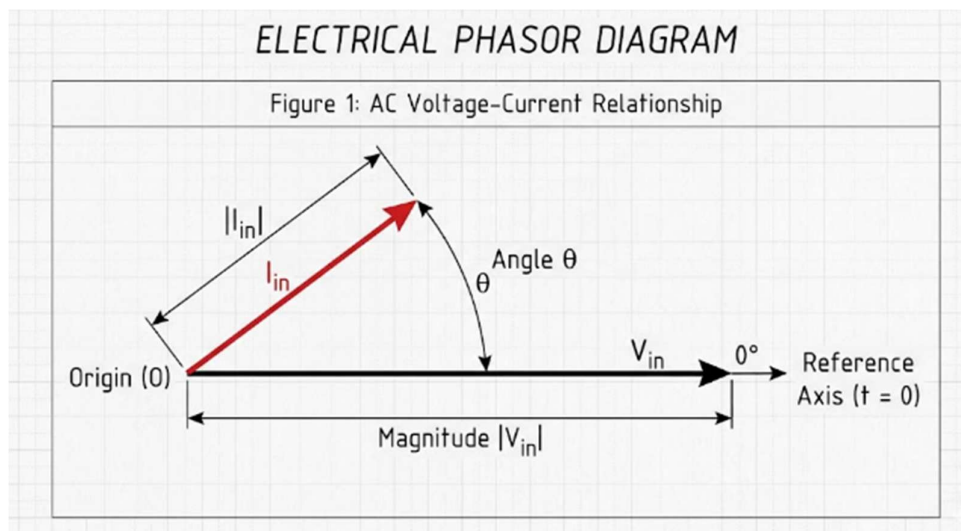
$$V_R = 174.0 \angle 13.3^\circ \text{ V}$$

Q-4: A current of 10 A leads the voltage by 30° , Represent the voltage and current phasors.

Answer:

Given: $I = 10 \text{ A}$, $\phi = 30^\circ$ (I leads V).

Phasor Diagram:



Q-5: A single-phase load takes 10 A current from 230 V supply at a power factor of 0.8 lagging. Calculate: (a) Active power, (b) Reactive power, (c) Apparent power

Answer:

Given:

$$I = 10 \text{ A}, V = 230 \text{ V}, \text{PF} = 0.8$$

To Find: (a) Active power P , (b) Reactive power Q , (c) Apparent power S

Formulas:

$$S = VI$$

$$P = S \cdot \text{PF}$$

$$Q = S \cdot \sin \phi, \sin \phi = \sqrt{1 - \text{PF}^2}$$

Solution:

$$S = 230 \times 10 = 2300 \text{ VA}$$

$$P = 2300 \times 0.8 = 1840 \text{ W}$$

$$\sin \phi = \sqrt{1 - 0.8^2} = 0.6$$

$$Q = 2300 \times 0.6 = 1380 \text{ VAR}$$

Final Answer:

$$P = 1840 \text{ W}, Q = 1380 \text{ VAR}, S = 2300 \text{ VA}$$

Q-6: A load absorbs 4 kW at a power factor of 0.6 lagging. Find the apparent power and reactive power.

Answer:

Given: $P = 4 \text{ kW}$, $\text{pf} = 0.6$ lagging

Apparent power:

$$S = \frac{P}{\text{pf}} = \frac{4}{0.6} \approx 6.667 \text{ kVA}$$

Reactive power:

$$Q = \sqrt{S^2 - P^2} = \sqrt{(6.667)^2 - (4)^2} \approx 5.333 \text{ kVAR}$$

Final Answer:

$$S \approx 6.67 \text{ kVA}, Q \approx 5.33 \text{ kVAR (lagging)}$$

Q-7: A resistor of 20 Ω is connected to 230 V, 50 Hz AC supply. Find the current and power consumed.

Answer:

Given:

$$R = 20 \Omega, V = 230 \text{ V}, f = 50 \text{ Hz}$$

To Find: Current I and power consumed P

Formulas:

$$I = \frac{V}{R}, P = I^2 R = \frac{V^2}{R}$$

Solution:

$$I = \frac{230}{20} = 11.5 \text{ A}$$

$$P = \frac{230^2}{20} = \frac{52900}{20} = 2645 \text{ W}$$

Final Answer:

$$I = 11.5 \text{ A}, P = 2645 \text{ W}$$

Q-8: A pure inductance of 0.2 H and a capacitor of 50 μF is connected to 230 V, 50 Hz supply. Calculate reactance of the circuit and current.

Answer:

Given: $L = 0.2 \text{ H}, C = 50 \mu\text{F}, V = 230 \text{ V}, f = 50 \text{ Hz}$

Inductive reactance:

$$X_L = 2\pi fL = 2\pi(50)(0.2) = 62.83 \Omega$$

Capacitive reactance:

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(50)(50 \times 10^{-6})} \approx 63.66 \Omega$$

Since L and C are in series:

$$X = X_L - X_C = 62.83 - 63.66 = -0.83 \Omega$$

(Net capacitive reactance)

Impedance magnitude:

$$|Z| = \sqrt{0^2 + (0.83)^2} \approx 0.83 \Omega$$

Current:

$$I = \frac{V}{|Z|} = \frac{230}{0.83} \approx 277.11 \text{ A}$$

Final Answer:

$$X \approx 0.83 \Omega \text{ (capacitive)}, I \approx 277.1 \text{ A}$$

Q-9: An RL series circuit has $R = 10 \Omega$ and $L = 0.1 \text{ H}$. If supply voltage is 230 V at 50 Hz, find current and power factor.

Answer:

Given:

$$R = 10 \Omega, L = 0.1 \text{ H}, V = 230 \text{ V}, f = 50 \text{ Hz}$$

To Find: Current I and power factor PF

Formulas:

$$X_L = 2\pi fL, Z = \sqrt{R^2 + X_L^2}, I = \frac{V}{Z}, \text{PF} = \frac{R}{Z}$$

Solution:

$$\begin{aligned} X_L &= 2\pi(50)(0.1) = 31.416 \Omega \\ Z &= \sqrt{10^2 + 31.416^2} = \sqrt{100 + 986.6} = \sqrt{1086.6} = 32.97 \Omega \\ I &= \frac{230}{32.97} = 6.976 \text{ A} \\ \text{PF} &= \frac{10}{32.97} = 0.303 \text{ lagging} \end{aligned}$$

Final Answer:

$$I = 6.98 \text{ A}, \text{PF} = 0.303 \text{ lagging}$$

Q-10: In a series RC circuit, $R = 20 \Omega$ and $C = 100 \mu\text{F}$. Find impedance, current and phase angle.

Answer:

Given: $R = 20 \Omega, C = 100 \times 10^{-6} \text{ F}$

Assume frequency $f = 50 \text{ Hz}$ (typical for such problems unless specified).

Capacitive reactance:

$$X_C = \frac{1}{2\pi(50)(100 \times 10^{-6})} \approx 31.83 \Omega$$

Impedance:

$$Z = R - jX_C = 20 - j31.83$$

Magnitude:

$$|Z| = \sqrt{20^2 + 31.83^2} \approx 37.59 \Omega$$

Phase angle:

$$\phi = -\tan^{-1}\left(\frac{31.83}{20}\right) \approx -57.87^\circ$$

Assuming voltage V given, if not, current in terms of V is:

$$I = \frac{V}{|Z|}, \text{ leads voltage by } 57.87^\circ.$$

Final Answer:

$$|Z| \approx 37.59 \Omega, \phi \approx -57.87^\circ$$

Q-11: In a parallel RC circuit, $R = 40 \Omega$ and $C = 100 \mu\text{F}$. Find line current and phase angle.

Answer:

Given:

$$R = 40 \Omega, C = 100 \times 10^{-6} \text{ F}, V = 230 \text{ V}, f = 50 \text{ Hz}$$

To Find: Line current I_L and phase angle ϕ

Formulas:

$$X_C = \frac{1}{2\pi f C}, I_R = \frac{V}{R}, I_C = \frac{V}{X_C}$$

$$I_L = \sqrt{I_R^2 + I_C^2}, \phi = \tan^{-1}\left(\frac{I_C}{I_R}\right)$$

Solution:

$$X_C = \frac{1}{2\pi(50)(100 \times 10^{-6})} = \frac{1}{0.031416} = 31.83 \Omega$$

$$I_R = \frac{230}{40} = 5.75 \text{ A}$$

$$I_C = \frac{230}{31.83} = 7.226 \text{ A}$$

$$I_L = \sqrt{(5.75)^2 + (7.226)^2} = \sqrt{33.06 + 52.22} = \sqrt{85.28} = 9.235 \text{ A}$$

$$\phi = \tan^{-1}\left(\frac{7.226}{5.75}\right) = \tan^{-1}(1.257) = 51.5^\circ \text{ (leading)}$$

Final Answer:

$$I_L = 9.24 \text{ A}, \phi = 51.5^\circ \text{ leading}$$

Q-12: A resistor of 40Ω and an inductor of 0.2 H and capacitor of $120 \mu\text{F}$ are connected in parallel across 230 V , 50 Hz supply. Find (1) the current of each branch (2) the resultant current (3) Power factor of the circuit

Answer:

Given: $R = 40 \Omega$, $L = 0.2 \text{ H}$, $C = 120 \mu\text{F}$, $V = 230 \text{ V}$, $f = 50 \text{ Hz}$

Branch currents:

$$I_R = \frac{V}{R} = \frac{230}{40} = 5.75 \text{ A (in phase)}$$

$$X_L = 2\pi(50)(0.2) = 62.83 \Omega, I_L = \frac{230}{62.83} \approx 3.66 \text{ A (lags } 90^\circ)$$

$$X_C = \frac{1}{2\pi(50)(120 \times 10^{-6})} \approx 26.53 \Omega, I_C = \frac{230}{26.53} \approx 8.67 \text{ A (leads } 90^\circ)$$

Net reactive current:

$$I_X = I_C - I_L = 8.67 - 3.66 = 5.01 \text{ A (leading)}$$

Resultant current:

$$I = \sqrt{I_R^2 + I_X^2} = \sqrt{(5.75)^2 + (5.01)^2} \approx 7.63 \text{ A}$$

Power factor:

$$pf = \frac{I_R}{I} = \frac{5.75}{7.63} \approx 0.754 \text{ leading}$$

Final Answer:

$$I_R = 5.75 \text{ A}, I_L = 3.66 \text{ A}, I_C = 8.67 \text{ A}, I = 7.63 \text{ A}, pf \approx 0.754 \text{ leading}$$

Q-13: A R-C series circuit having Resistance $R = 5.77 \Omega$ and reactance $X_C = 3.33 \Omega$ is connected across 230 V , 50 Hz ac supply. Find (a) current (b) Power factor (c) Average power.

Answer:

Given:

$R = 5.77 \Omega$, $X_C = 3.33 \Omega$, $V = 230 \text{ V}$, $f = 50 \text{ Hz}$

To Find: (a) Current I , (b) Power factor PF, (c) Average power P

Formulas:

$$Z = \sqrt{R^2 + X_C^2}, I = \frac{V}{Z}, \text{PF} = \frac{R}{Z}, P = I^2 R$$

Solution:

$$Z = \sqrt{(5.77)^2 + (3.33)^2} = \sqrt{33.29 + 11.09} = \sqrt{44.38} = 6.662 \Omega$$

$$I = \frac{230}{6.662} = 34.52 \text{ A}$$

$$\text{PF} = \frac{5.77}{6.662} = 0.866 \text{ leading}$$

$$P = (34.52)^2 \times 5.77 = 1191.5 \times 5.77 = 6872 \text{ W}$$

Final Answer:

$$I = 34.5 \text{ A}, \text{PF} = 0.866 \text{ leading}, P = 6872 \text{ W}$$

Q-14: A circuit consumes a power of 1000 W at 0.6 leading power factor, when connected to 200 V, 50 Hz ac supply. Calculate (a) Current (b) Apparent power (c) Reactive power.

Answer:

Given: $P = 1000 \text{ W}$, $\text{pf} = 0.6 \text{ leading}$, $V = 200 \text{ V}$

(a) Current:

$$P = VI \cos \phi \Rightarrow I = \frac{P}{V \cos \phi} = \frac{1000}{200 \times 0.6} \approx 8.333 \text{ A}$$

(b) Apparent power:

$$S = VI = 200 \times 8.333 \approx 1666.67 \text{ VA}$$

(c) Reactive power:

$$Q = \sqrt{S^2 - P^2} = \sqrt{1666.67^2 - 1000^2} \approx 1333.33 \text{ VAR (leading)}$$

Final Answer:

$$I = 8.33 \text{ A}, S = 1666.67 \text{ VA}, Q \approx 1333.33 \text{ VAR (leading)}$$

Q-15: In a series-parallel circuit, the parallel branches A and B are in series with branch C. The impedances are: $Z_A = (4 + j3) \Omega$, $Z_B = (4 - j316) \Omega$, $Z_C = (2 + j8) \Omega$, If the

current $I_C = (25 + j0)$ Amp, Determine the branch currents and voltages and the total voltage. Hence calculate the complex power for each branch and the whole circuit.

Answer:

Given:

$$Z_A = (4 + j3) \Omega$$

$$Z_B = (4 - j316) \Omega$$

$$Z_C = (2 + j8) \Omega$$

$$I_C = 25 \angle 0^\circ \text{ A} = 25 + j0 \text{ A}$$

Step 1: Voltage across branch C

$$V_C = I_C \times Z_C = 25 \times (2 + j8) = 50 + j200 \text{ V}$$

Magnitude:

$$|V_C| = \sqrt{50^2 + 200^2} = \sqrt{2500 + 40000} = \sqrt{42500} \approx 206.16 \text{ V}$$

Step 2: Equivalent impedance of parallel branches A and B

$$Y_A = \frac{1}{Z_A} = \frac{1}{4 + j3} = \frac{4 - j3}{25} = 0.16 - j0.12 \text{ S}$$

$$Y_B = \frac{1}{Z_B} = \frac{1}{4 - j316} = \frac{4 + j316}{(4)^2 + (316)^2}$$

$$(4)^2 + (316)^2 = 16 + 99856 = 99872$$

$$Y_B = \frac{4 + j316}{99872} \approx 4.004 \times 10^{-5} + j0.003163 \text{ S}$$

$$Y_{AB} = Y_A + Y_B \approx (0.16 + 4.004 \times 10^{-5}) + j(-0.12 + 0.003163)$$

$$Y_{AB} \approx 0.16004 - j0.116837 \text{ S}$$

$$Z_{AB} = \frac{1}{Y_{AB}} \approx \frac{1}{0.16004 - j0.116837}$$

Let's compute magnitude and phase of Y_{AB} :

$$|Y_{AB}| = \sqrt{(0.16004)^2 + (0.116837)^2} \approx \sqrt{0.025613 + 0.013651} \approx \sqrt{0.039264} \approx 0.19815 \text{ S}$$

$$\theta_Y = \tan^{-1} \left(\frac{-0.116837}{0.16004} \right) \approx \tan^{-1}(-0.730) \approx -36.1^\circ$$

$$|Z_{AB}| = \frac{1}{0.19815} \approx 5.046 \Omega$$

$$\theta_Z = -\theta_Y = 36.1^\circ$$

So:

$$Z_{AB} \approx 5.046 \angle 36.1^\circ \Omega$$

In rectangular:

$$Z_{AB} \approx 5.046 \cos 36.1^\circ + j5.046 \sin 36.1^\circ \approx 4.08 + j2.976 \Omega$$

Step 3: Voltage across parallel branches A and B

$$\begin{aligned} V_{AB} &= I_C \times Z_{AB} = 25 \times (4.08 + j2.976) = 102 + j74.4 \text{ V} \\ |V_{AB}| &= \sqrt{102^2 + 74.4^2} \approx \sqrt{10404 + 5535} \approx \sqrt{15939} \approx 126.25 \text{ V} \end{aligned}$$

Step 4: Branch currents A and B

$$I_A = \frac{V_{AB}}{Z_A} = \frac{102 + j74.4}{4 + j3}$$

Multiply numerator and denominator by $4 - j3$:

$$(102 + j74.4)(4 - j3) = 408 - j306 + j297.6 + 223.2$$

Wait — carefully:

$$\begin{aligned} (102 + j74.4)(4 - j3) &= 102 \cdot 4 + 102 \cdot (-j3) + j74.4 \cdot 4 + j74.4 \cdot (-j3) \\ &= 408 - j306 + j297.6 + 223.2 \\ \text{Real: } &408 + 223.2 = 631.2 \\ \text{Imag: } &-306 + 297.6 = -8.4 \end{aligned}$$

Denominator: $4^2 + 3^2 = 25$

$$\begin{aligned} I_A &= \frac{631.2 - j8.4}{25} = 25.248 - j0.336 \text{ A} \\ |I_A| &\approx \sqrt{25.248^2 + 0.336^2} \approx 25.25 \text{ A} \\ I_B &= \frac{V_{AB}}{Z_B} = \frac{102 + j74.4}{4 - j3} \end{aligned}$$

Multiply numerator and denominator by $4 + j3$:

Numerator:

$$\begin{aligned}
 (102 + j74.4)(4 + j316) &= 408 + j102 \cdot 316 + j74.4 \cdot 4 + j^2 \cdot 74.4 \cdot 316 \\
 &= 408 + j32232 + j297.6 - 23510.4 \\
 \text{Real: } 408 - 23510.4 &= -23102.4 \\
 \text{Imag: } 32232 + 297.6 &= 32529.6
 \end{aligned}$$

So numerator: $-23102.4 + j32529.6$

Denominator: $4^2 + 316^2 = 16 + 99856 = 99872$

$$\begin{aligned}
 I_B &= \frac{-23102.4 + j32529.6}{99872} \\
 &\approx -0.2313 + j0.3256 \text{ A} \\
 |I_B| &\approx \sqrt{0.05348 + 0.10601} \approx \sqrt{0.15949} \approx 0.3994 \text{ A}
 \end{aligned}$$

Step 5: Total voltage V_T

$$\begin{aligned}
 V_T = V_{AB} + V_C &= (102 + j74.4) + (50 + j200) = 152 + j274.4 \text{ V} \\
 |V_T| &= \sqrt{152^2 + 274.4^2} \approx \sqrt{23104 + 75295} \approx \sqrt{98399} \approx 313.7 \text{ V}
 \end{aligned}$$

Step 6: Complex power for each branch

Branch C:

$$S_C = V_C \times I_C^*$$

$$I_C^* = 25 - j0$$

$$S_C = (50 + j200) \times 25 = 1250 + j5000 \text{ VA}$$

Branch A:

$$S_A = V_{AB} \times I_A^*$$

$$I_A^* = 25.248 + j0.336$$

$$V_{AB} = 102 + j74.4$$

$$S_A = (102 + j74.4)(25.248 + j0.336)$$

Multiply:

$$\text{Real: } 102 \times 25.248 + 74.4 \times 0.336 = 2575.3 + 24.998 \approx 2600.3$$

$$\text{Imag: } 102 \times 0.336 + 74.4 \times 25.248 = 34.272 + 1878.45 \approx 1912.7$$

$$S_A \approx 2600.3 + j1912.7 \text{ VA}$$

Branch B:

$$S_B = V_{AB} \times I_B^*$$

$$I_B^* = -0.2313 - j0.3256$$

$$S_B = (102 + j74.4)(-0.2313 - j0.3256)$$

Multiply:

$$\text{Real: } 102 \times (-0.2313) + 74.4 \times (-0.3256) = -23.59 - 24.21 \approx -47.80$$

$$\text{Imag: } 102 \times (-0.3256) + 74.4 \times (-0.2313) = -33.21 - 17.21 \approx -50.42$$

$$S_B \approx -47.80 - j50.42 \text{ VA}$$

Whole circuit:

$$S_{\text{total}} = S_A + S_B + S_C$$

$$\text{Real: } 2600.3 - 47.80 + 1250 = 3802.5$$

$$\text{Imag: } 1912.7 - 50.42 + 5000 = 6862.28$$

$$S_{\text{total}} \approx 3802.5 + j6862.3 \text{ VA}$$

Final Answers:

$$I_A \approx 25.25 \text{ A}, I_B \approx 0.399 \text{ A}$$

$$V_A = V_B = V_{AB} \approx 126.3 \text{ V}, V_C \approx 206.2 \text{ V}, V_T \approx 313.7 \text{ V}$$

$$S_A \approx 2600 + j1913 \text{ VA}, S_B \approx -47.8 - j50.4 \text{ VA}, S_C = 1250 + j5000 \text{ VA}, S_{\text{total}} \approx 3803 + j6862 \text{ VA}$$

Q-16: Two impedances are connected in parallel across a 100 volt, 50 Hz a.c. supply. Impedance no. 1 has resistance of 8 Ω and capacitive reactance of 7 Ω . While impedance no. 2 has resistance of 5 Ω and inductive reactance of 6 Ω . Calculate: (i) Current through each circuit & p.f. of each circuit. (ii) Total current and p.f. of combined circuit. (iii) Power taken by the whole circuit.

Answer:

Given:

$$Z_1 = 8 - j7 \Omega, Z_2 = 5 + j6 \Omega, V = 100 \text{ V}$$

(i) Current through each circuit & pf:

$$I_1 = \frac{V}{|Z_1|} = \frac{100}{\sqrt{8^2 + 7^2}} = \frac{100}{\sqrt{113}} \approx 9.41 \text{ A}$$

$$\text{pf}_1 = \cos \phi_1 = \frac{8}{\sqrt{113}} \approx 0.754 \text{ leading (since capacitive).}$$

$$I_2 = \frac{V}{|Z_2|} = \frac{100}{\sqrt{5^2 + 6^2}} = \frac{100}{\sqrt{61}} \approx 12.81 \text{ A}$$

$$\text{pf}_2 = \frac{5}{\sqrt{61}} \approx 0.64 \text{ lagging (inductive).}$$

(ii) Total current & pf:

Admittances:

$$Y_1 = \frac{1}{Z_1} = \frac{1}{8 - j7} = \frac{8 + j7}{113} \approx 0.0708 + j0.0619 \text{ S}$$

$$Y_2 = \frac{1}{Z_2} = \frac{1}{5 + j6} = \frac{5 - j6}{61} \approx 0.0820 - j0.0984 \text{ S}$$

$$Y_T = Y_1 + Y_2 \approx 0.1528 - j0.0365 \text{ S}$$

$$|Y_T| \approx 0.1565 \text{ S}$$

$$I_T = V \times |Y_T| = 100 \times 0.1565 \approx 15.65 \text{ A}$$

$$\phi_T = \tan^{-1} \left(\frac{-0.0365}{0.1528} \right) \approx -13.43^\circ$$

$$\text{pf}_T = \cos \phi_T \approx 0.973 \text{ leading.}$$

(iii) Power taken:

$$P = VI_T \cos \phi_T = 100 \times 15.65 \times 0.973 \approx 1522.5 \text{ W}$$

Final Answer:

$$I_1 \approx 9.41 \text{ A (0.754 leading)}, I_2 \approx 12.81 \text{ A (0.64 lagging)}, I_T \approx 15.65 \text{ A, pf}_T \approx 0.973 \text{ leading, } P \approx 1522.5 \text{ W}$$

Q-17: A series RLC circuit consists of a resistance of 500 Ω , inductance of 50 mH and a capacitance of 20 pF. Find: (i) The resonant frequency, (ii) The Q factor of the circuit of resonance, (iii) The half power frequency

Answer:

Given:

$$R = 500 \Omega$$

$$L = 50 \times 10^{-3} \text{ H}$$

$$C = 20 \times 10^{-12} \text{ F}$$

To Find:

- (i) Resonant frequency f_r
- (ii) Quality factor Q at resonance
- (iii) Half-power frequencies f_1, f_2

(i) Resonant frequency

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

$$LC = 50 \times 10^{-3} \times 20 \times 10^{-12} = 1000 \times 10^{-15} = 1 \times 10^{-12}$$

$$\sqrt{LC} = 1 \times 10^{-6}$$

$$f_r = \frac{1}{2\pi \times 10^{-6}} \approx 159154.94 \text{ Hz}$$

$$\boxed{f_r \approx 159.15 \text{ kHz}}$$

(ii) Quality factor Q

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$\frac{L}{C} = \frac{50 \times 10^{-3}}{20 \times 10^{-12}} = 2.5 \times 10^9$$

$$\sqrt{\frac{L}{C}} = \sqrt{2.5 \times 10^9} \approx 50000$$

$$Q = \frac{50000}{500} = 100$$

$$\boxed{Q = 100}$$

(iii) Half-power frequencies

For high $Q > 10$, approximate formulas:

$$f_1 \approx f_r - \frac{BW}{2}, f_2 \approx f_r + \frac{BW}{2}$$

Bandwidth:

$$BW = \frac{f_r}{Q} = \frac{159154.94}{100} \approx 1591.55 \text{ Hz}$$

$$f_1 \approx 159154.94 - 795.775 \approx 158359.17 \text{ Hz}$$

$$f_2 \approx 159154.94 + 795.775 \approx 159950.72 \text{ Hz}$$

$$\boxed{f_1 \approx 158.36 \text{ kHz}, f_2 \approx 159.95 \text{ kHz}}$$

Q-18: A resistance of 1Ω and inductance of 0.02 H are connected in series with a capacitor across 200 V supply. Find the value of capacitance, so that current drawn by circuit will be maximum at frequency 50 Hz . Find current and voltage across capacitor.

Answer:

Given: $R = 1 \Omega, L = 0.02 \text{ H}, V = 200 \text{ V}, f = 50 \text{ Hz}$

For max current at resonance:

$$\omega_r L = \frac{1}{\omega_r C} \Rightarrow C = \frac{1}{\omega_r^2 L} = \frac{1}{(2\pi \times 50)^2 \times 0.02}$$

$$C = \frac{1}{(314.16)^2 \times 0.02} \approx \frac{1}{1973.9} \approx 5.066 \times 10^{-4} \text{ F} = 506.6 \mu\text{F}$$

At resonance, $Z = R = 1 \Omega$

$$I_{\max} = \frac{V}{R} = \frac{200}{1} = 200 \text{ A}$$

Voltage across capacitor:

$$V_C = I \times X_C = 200 \times \frac{1}{2\pi(50)(506.6 \times 10^{-6})}$$

$$X_C = \frac{1}{314.16 \times 5.066 \times 10^{-4}} \approx 6.28 \Omega$$

$$V_C \approx 200 \times 6.28 = 1256 \text{ V}$$

Final Answer:

$$\boxed{C \approx 506.6 \mu\text{F}, I_{\max} = 200 \text{ A}, V_C \approx 1256 \text{ V}}$$

Q-19: A balanced star connected load of $(8 + j6) \Omega$ per phase is connected to a 415 V , 50 Hz , $3\text{-}\phi$ supply. Find the line current, power factor, power and total volt-amps.

Answer:

Given:

$$Z_{\text{ph}} = 8 + j6 \Omega$$

$$V_L = 415 \text{ V}$$

Star connection

To Find:

Line current I_L , power factor, total power P , total VA

Step 1: Phase voltage

$$\text{Star: } V_{\text{ph}} = \frac{V_L}{\sqrt{3}} = \frac{415}{\sqrt{3}} \approx 239.6 \text{ V}$$

Step 2: Phase impedance magnitude

$$|Z_{\text{ph}}| = \sqrt{8^2 + 6^2} = \sqrt{64 + 36} = 10 \Omega$$

Step 3: Phase current = Line current (star)

$$I_{\text{ph}} = I_L = \frac{V_{\text{ph}}}{|Z_{\text{ph}}|} = \frac{239.6}{10} = 23.96 \text{ A}$$

Step 4: Power factor

$$\text{PF} = \frac{R}{|Z_{\text{ph}}|} = \frac{8}{10} = 0.8 \text{ lagging}$$

Step 5: Total power

3-phase power:

$$P = \sqrt{3}V_L I_L \times \text{PF} = \sqrt{3} \times 415 \times 23.96 \times 0.8$$

$$P \approx 1.732 \times 415 \times 23.96 \times 0.8 \approx 13800 \text{ W}$$

Step 6: Total volt-amps

$$S = \sqrt{3}V_L I_L = 1.732 \times 415 \times 23.96 \approx 17250 \text{ VA}$$

Final Answer:

$$I_L = 24.0 \text{ A, PF} = 0.8 \text{ lagging, } P \approx 13.8 \text{ kW, } S \approx 17.25 \text{ kVA}$$

Q-20: For 3- ϕ star connected load consists of non-inductive resistance of 50 Ω in parallel with a capacitance of 15 μF . Calculate the line current, power absorbed, total kVA and power factor when connected to 415 V, 3 phase, 50 Hz supply.

Answer:

Given: Per phase: $R = 50 \Omega$, $C = 15 \mu\text{F}$, $V_L = 415 \text{ V}$

Phase voltage:

$$V_{\text{ph}} = \frac{V_L}{\sqrt{3}} = \frac{415}{\sqrt{3}} \approx 239.6 \text{ V}$$

Admittance per phase:

$$Y = \frac{1}{R} + j\omega C = \frac{1}{50} + j(2\pi \times 50 \times 15 \times 10^{-6})$$

$$Y = 0.02 + j0.004712 \approx 0.02055 \angle 13.24^\circ \text{ S}$$

Phase current:

$$I_{ph} = V_{ph} \times |Y| = 239.6 \times 0.02055 \approx 4.925 \text{ A}$$

Line current = phase current for star:

$$I_L \approx 4.925 \text{ A}$$

Power absorbed per phase:

$$P_{ph} = V_{ph}^2 \times G = (239.6)^2 \times 0.02 \approx 1148.3 \text{ W}$$

Total power:

$$P_T = 3 \times P_{ph} \approx 3444.9 \text{ W}$$

Total kVA:

$$S_T = 3 \times V_{ph} I_{ph} = 3 \times 239.6 \times 4.925 \approx 3539.6 \text{ VA} = 3.54 \text{ kVA}$$

Power factor:

$$pf = \cos(13.24^\circ) \approx 0.973 \text{ leading}$$

Final Answer:

$$I_L \approx 4.925 \text{ A}, P_T \approx 3.445 \text{ kW}, S_T \approx 3.54 \text{ kVA}, pf \approx 0.973 \text{ leading}$$

Q-21: A 3- ϕ load consists of three similar inductive coils, having resistance 50 Ω and inductance 0.2 H. If Supply Voltage is 415 V, 50 Hz, calculate: (i) the line current (ii) power factor (iii) total power consumed when load is connected in star and delta.

Answer:

Given per coil:

$$R = 50 \Omega$$

$$L = 0.2 \text{ H}$$

$$f = 50 \text{ Hz}$$

$$X_L = 2\pi fL = 2\pi \times 50 \times 0.2 = 62.832 \Omega$$

$$Z_{\text{ph}} = 50 + j62.832 \Omega$$

$$|Z_{\text{ph}}| = \sqrt{50^2 + 62.832^2} \approx 80.3 \Omega$$

(i) & (ii) & (iii) for Star connection

Phase voltage:

$$V_{\text{ph}} = \frac{V_L}{\sqrt{3}} = \frac{415}{\sqrt{3}} \approx 239.6 \text{ V}$$

Phase current:

$$I_{\text{ph}} = \frac{V_{\text{ph}}}{|Z_{\text{ph}}|} = \frac{239.6}{80.3} \approx 2.984 \text{ A}$$

Star: $I_L = I_{\text{ph}} \approx 2.984 \text{ A}$

Power factor:

$$\text{PF} = \frac{R}{|Z_{\text{ph}}|} = \frac{50}{80.3} \approx 0.622 \text{ lagging}$$

Total power:

$$P = 3 \times I_{\text{ph}}^2 \times R = 3 \times (2.984)^2 \times 50$$

$$P \approx 3 \times 8.904 \times 50 \approx 1335.6 \text{ W}$$

or

$$P = \sqrt{3} V_L I_L \times \text{PF} = 1.732 \times 415 \times 2.984 \times 0.622 \approx 1335 \text{ W}$$

For Delta connection

Phase voltage = Line voltage:

$$V_{\text{ph}} = 415 \text{ V}$$

Phase current:

$$I_{\text{ph}} = \frac{415}{80.3} \approx 5.168 \text{ A}$$

Line current:

$$I_L = \sqrt{3} \times I_{ph} = 1.732 \times 5.168 \approx 8.952 \text{ A}$$

Power factor same: PF \approx 0.622 lagging

Total power:

$$P = 3 \times I_{ph}^2 \times R = 3 \times (5.168)^2 \times 50$$

$$P \approx 3 \times 26.71 \times 50 \approx 4006.5 \text{ W}$$

Final Answer:

Star:

$$I_L \approx 2.98 \text{ A, PF} \approx 0.622, P \approx 1.34 \text{ kW}$$

Delta:

$$I_L \approx 8.95 \text{ A, PF} \approx 0.622, P \approx 4.01 \text{ kW}$$

Q-22: In balanced 3- ϕ , 415 V system, line current is 100 A. When power is measured by two wattmeters, one wattmeter indicates power and other indicates zero. What will be power factor of load & measured power? If the power factor were unity and same load current what would be the reading of each wattmeter?

Answer:

Given: $V_L = 415 \text{ V}, I_L = 100 \text{ A}, W_1 = \text{some } P, W_2 = 0$

When one wattmeter reads zero:

$$W_2 = 0 \Rightarrow \cos(\phi - 30^\circ) = 0 \Rightarrow \phi - 30^\circ = 90^\circ \Rightarrow \phi = 120^\circ$$

But pf angle $\leq 90^\circ$ for loads. Actually, for $W_2 = 0$,

$$\phi = 60^\circ \text{ (since } W = V_L I_L \cos(\phi \pm 30^\circ))$$

Check:

$$W_2 = V_L I_L \cos(\phi + 30^\circ) = 0 \Rightarrow \phi + 30^\circ = 90^\circ \Rightarrow \phi = 60^\circ$$

Power factor:

$$pf = \cos 60^\circ = 0.5 \text{ lagging}$$

Measured power:

$$P_T = W_1 + W_2 = W_1 + 0 = V_L I_L \cos(\phi - 30^\circ) \times 2?$$

Better: $P_T = \sqrt{3} V_L I_L \cos \phi$

$$P_T = \sqrt{3} \times 415 \times 100 \times 0.5 \approx 35938.5 \text{ W} = 35.94 \text{ kW}$$

If pf were unity ($\phi = 0$):

Each wattmeter reading:

$$W = V_L I_L \cos(30^\circ) = 415 \times 100 \times \frac{\sqrt{3}}{2} \approx 35938.5/2?$$

Actually:

$$W_1 = V_L I_L \cos(30^\circ) \approx 35938.5 \text{ W}/\sqrt{3}?$$

Let's compute:

$$W = 415 \times 100 \times \cos(30^\circ) \approx 415 \times 100 \times 0.866 \approx 35939 \text{ W? That's too high.}$$

Wait: For unity pf, total power $P_T = \sqrt{3} \times 415 \times 100 \times 1 \approx 71877 \text{ W}$.

Each wattmeter reads:

$$W = V_L I_L \cos(30^\circ) = 415 \times 100 \times 0.866 \approx 35938.5 \text{ W}$$

Thus $W_1 = W_2 \approx 35.94 \text{ kW}$.

Final Answer:

pf = 0.5 lagging, $P_T \approx 35.94 \text{ kW}$, At unity pf: each wattmeter reads $\approx 35.94 \text{ kW}$

Q-23: For 415 V, three phase system, power was measured by two wattmeters and readings were 10.5 kW and -2.5 kW. Calculate (i) power factor (ii) Line current.

Answer:

Given:

$$W_1 = 10.5 \text{ kW}$$

$$W_2 = -2.5 \text{ kW}$$

(i) Power factor

Total power:

$$\begin{aligned}
 P &= W_1 + W_2 = 10.5 - 2.5 = 8.0 \text{ kW} \\
 \tan \phi &= \sqrt{3} \cdot \frac{W_1 - W_2}{W_1 + W_2} = \sqrt{3} \cdot \frac{10.5 - (-2.5)}{8.0} \\
 &= \sqrt{3} \cdot \frac{13.0}{8.0} = 1.732 \times 1.625 = 2.8145 \\
 \phi &= \tan^{-1}(2.8145) \approx 70.5^\circ \\
 \text{PF} &= \cos \phi \approx \cos 70.5^\circ \approx 0.333
 \end{aligned}$$

(ii) Line current

$$\begin{aligned}
 P &= \sqrt{3} V_L I_L \times \text{PF} \\
 8000 &= 1.732 \times 415 \times I_L \times 0.333 \\
 I_L &= \frac{8000}{1.732 \times 415 \times 0.333} \approx \frac{8000}{239.5} \approx 33.4 \text{ A}
 \end{aligned}$$

Final Answer:

$$\boxed{\text{PF} \approx 0.333, I_L \approx 33.4 \text{ A}}$$
