

GUJARAT TECHNOLOGICAL UNIVERSITY

BACHELOR OF ENGINEERING – SEMESTER 7 – EXAMINATION – SUMMER 2026

Subject Code: 3170513

Date: 20/05/2026

Subject Name: Process Modelling, Simulation and Optimization

Time: 02:30 PM TO 05:00 PM

Total Marks: 70

Instructions:

- 1. Attempt all questions.**
- 2. Make suitable assumptions wherever necessary.**
- 3. Figures to the right indicate full marks.**
- 4. Simple and non-programmable scientific calculators are allowed.**

- Q.1**
- (a) List the various professional simulators used in chemical engineering. **03**
 - (b) Describe briefly the fundamental laws used in mathematical models of chemical engineering systems. **04**
 - (c) Explain the steps for solving optimization problems. Enlist the general obstacles faced while solving optimization problems. **07**

- Q.2**
- (a) Define: black-box model, white box model, gray model. **03**
 - (b) Differentiate between design mode and analysis mode in process simulation with a diagram. **04**
 - (c) Discuss the role of optimization in design and operation of binary distillation column with a focus on optimum reflux ratio. **07**

OR

- Q.2**
- (c) A closed cylindrical vessel can hold $20\pi \text{ m}^3$ of liquid. The material for the top and bottom costs \$10 per m^2 and material for the side costs \$8 per m^2 . Find the radius and height of the most economical vessel. **07**

- Q.3**
- (a) Find the values of x and z (both > 0) that maximize the function:
 $U = -x^2 + 10x + xz - z^2 + 8z + 2$ **03**
 - (b) Minimize $f(x) = x^2 - x$ by Newtons method and Secant method. Use the starting point in the range of -3 to +3. Compare the methods. **04**
 - (c) Minimize the function $f(x) = x^2 + \frac{54}{x}$ between the interval [2, 5] using (i) Bisection search method, (ii) Golden section search method. Compare the methods. **07**

OR

- Q.3**
- (a) List the application of optimization in chemical engineering. **03**
 - (b) Find the extreme points of the function and classify them.
 $f(x) = x_1^3 + x_2^3 + 2x_1^2 + 4x_2^2 + 6$ **04**
 - (c) Solve the following Linear Programming Problem by Simplex method. **07**
 Maximize $Z = 5x_1 + 3x_2$
 subject to:
 $x_1 + x_2 \leq 2$
 $5x_1 + 2x_2 \leq 10$
 $3x_1 + 8x_2 \leq 12$
 $x_1, x_2 \geq 0$

- Q.4** (a) Elaborate the process to build a model. **03**
 (b) Derive the model equations for two heated tanks. **04**
 (c) An oven is tested for heating and the following set of time and temperature data is collected. Fit the data to the equation, $T = a + bt$ where a and b are constants. **07**

t in min	1	2	3	4	5
T in $^{\circ}\text{C}$	12.5	21.4	31.8	42.1	53.5

OR

- Q.4** (a) Explain Random search method for multivariable optimization and its importance. **03**
 (b) Minimize the function $f(x) = 8x_1^2 + 5x_2^2 + 4x_1x_2$ using Newtons method. Take starting point $X_0 = [10,10]$. **04**
 (c) Develop a model for batch reactor. State the assumptions clearly. **07**

- Q.5** (a) Differentiate between steady state versus dynamic simulation. **03**
 (b) Explain equation solving approach with an example. **04**
 (c) Develop a model for mixing tank. State the assumptions. **07**

OR

- Q.5** (a) Write short note on decomposition of networks. **03**
 (b) Minimize $f(x) = 4x_1^2 + 5x_2^2$ subject to $2x_1 + 3x_2 = 6$ using Lagrange multiplier method. **04**
 (c) Write about partition and tearing applied to process flow sheeting. Explain any tearing algorithm with a flowchart. Write the steps clearly. **07**
