

Aptitude and Reasoning

P and C (Permutation & Combination)

F.P.C. → Fundamental principle of counting

↳ 25 Qns
out of 30 Qns

F.P.C. → Additive Rule

only one thing at a time

10 Boys 12 Girls

'a' monitor → 22 ways

$$10 + 12 = 22 \text{ ways}$$

'OR' → additive Rule can be applicable!

hidden in the meaning of question.

Product Rule

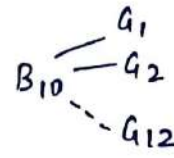
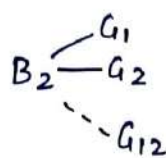
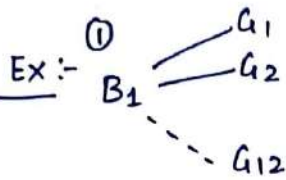
More than one thing

$$10 \times 12 = 120 \text{ ways}$$

1B & 1G monitor

and

qn. → hidden or given or available



$$10 \times 12 = 120$$



A → C

$$\frac{6 \text{ ways} + 3}{(3 \times 3)} = 9 \text{ ways}$$

* Arrangement

$${}^n P_r = \frac{n!}{(n-r)!}$$

6 chairs, 6 members.

Ex:- $\frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{1}$

$${}^6 P_6 = \frac{6!}{0!} = 720 \text{ ways}$$

if 2 chairs broken

$${}^6 P_4 = \frac{6!}{2!} = 360 \text{ ways}$$

Q → {a, b, c} → {ab, bc, ca}

selection

$${}^n C_r = \frac{n!}{(n-r)! \times r!}$$

$$\Rightarrow {}^3 C_2 = \frac{3!}{1! \times 2!} = 3 \text{ ways}$$

Q 12 people (handshake)

$${}^{12}C_2 = \frac{12!}{10! \times 2!} = \frac{12 \times 11}{2} = 66$$

$${}^nC_2 = \frac{n(n-1)}{2}$$

Q 12 points (str. line)

$${}^{12}C_2 = 66$$

* ${}^nC_r = {}^nC_{n-r} \rightarrow$ Ex:- ${}^5C_2 = {}^5C_3$
 ${}^8C_5 = {}^8C_3$

Q1> All 6 digit natural no's are being formed from 1st 6 natural no's without repetition. (w.r.n). How many such no's are divisible by 4?

Q2> How many 4 digit no. can be formed with 10 digits 0, 1, ..., 9. If no number can start with zero and if repetition are not allowed?

Q3> given digits 2, 2, 3, 3, 3, 4, 4, 4, 4. How many distinct 4 digit no's greater than 3000 can be formed?
 (Gate 2010) (a) 50 (b) 51 (c) 52 (d) 54.

Q4> All 4 digit natural no's are being formed from 1st five natural numbers. How many such no's are divisible by 4.

Me

Sol> ① $\frac{1}{\times} \frac{2}{\times} \frac{3}{\times} \frac{4}{\times} \frac{5}{\times} \frac{2}{\times} \quad (240)$

$\frac{1}{\times} \frac{2}{\times} \frac{3}{\times} \frac{4}{\times} \frac{5}{\times} \frac{6}{\times}$

②

$\frac{9}{\times} \frac{9}{\times} \frac{8}{\times} \frac{7}{\times}$

$0, 1, 2, 3, 4, 5, 6, 7, 8, 9$

$\frac{24}{\times 5} \quad (120) \checkmark$

$\begin{matrix} 56 \\ \times \\ 4 \times 3 \quad 12 \end{matrix}$

③

$\frac{2}{\times} \frac{7}{\times} \frac{6}{\times} \frac{5}{\times} = (5103) \frac{420}{1, 2, 3, 4, 5} \checkmark$

④

$\frac{5}{\times} \frac{5}{\times} \frac{5}{\times} \frac{1}{\times} \quad (250)$

$\frac{125}{\times} \quad (125) \checkmark$

- Sol $\rightarrow$ ① 192
 ② 4536
 ③ 51
 ④ 125

explanations

① $[1 \times 2 \times 3 \times 4] \times \begin{matrix} T & U \\ \hline & \end{matrix}$ $\rightarrow$ 8 ways
 1, 2, 3, 4, 5, 6

TU	TU	20	28
12	36	40	48
16	52	60	68
24	56	80	88
32	64	08	88
		04	8
		8	

44 ✓

$\Rightarrow 4 \times 3 \times 2 \times 1 \times 8 = 192 \text{ ways}$

② $\frac{9}{(1+9)} \times \frac{9}{(0+9)} \times \frac{8}{(0-9)} \times \frac{7}{(0-9)} = 4536$

④ $\frac{5}{(1+9)} \times \frac{5}{(0+9)} \times \begin{matrix} T & U \\ \hline & \end{matrix} \rightarrow 5$
 1, 2, 3, 4, 5

$\frac{125}{\text{Ans}}$
 1 2
 2 4
 3 2
 4 4
 5 2
 $\rightarrow$ 5 ways

③ (2, 2) (3, 3, 3) 4, 4, 4, 4

$\frac{1}{Th=3} \times \frac{3}{2 \text{ or } 3 \text{ or } 4} \times \frac{3}{2 \text{ or } 3 \text{ or } 4} \times \frac{3}{2 \text{ or } 3 \text{ or } 4}$
 $\rightarrow$ 27 ways
 such no's are there

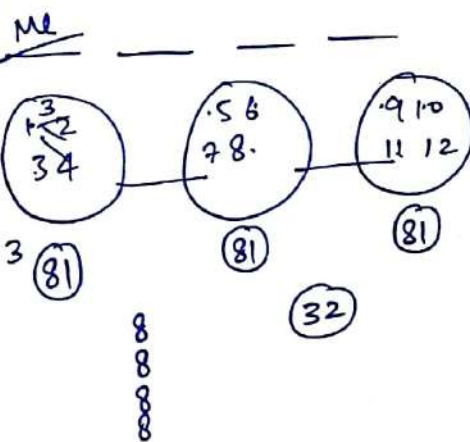
① 3222 but two 2's are allowed
 $\rightarrow$ invalid no. also 3333 ✓

other way

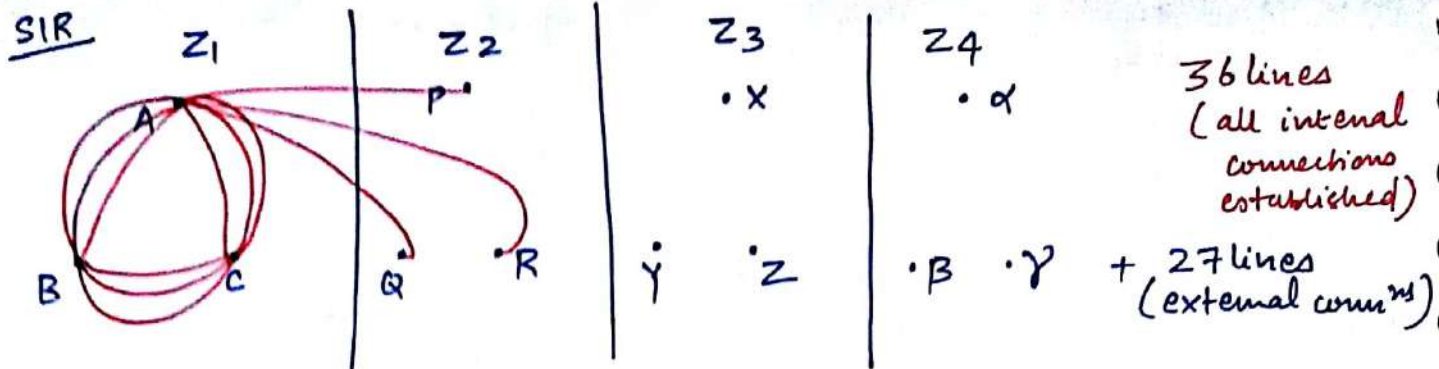
$\frac{2}{3/4} \frac{3}{2/3/4} \frac{3}{2/3/4} = \frac{54}{-3} = 51$

Q There are 12 towns equally to be divided into 4 zones. each town is connected to every other town in the same zone by 3 direct lines and each town is each town is connected to every other town outside the zone by single direct line. How many lines are to be laid/built?

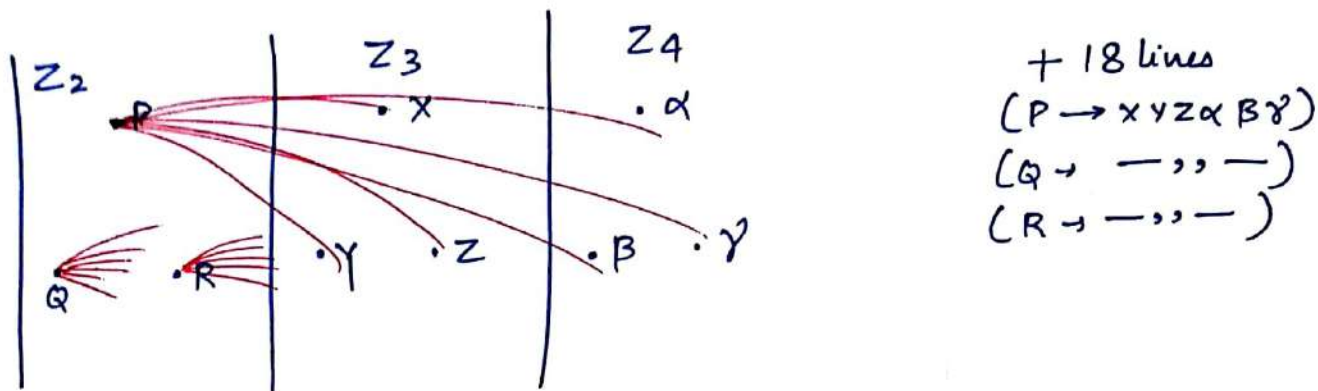
Sol 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12



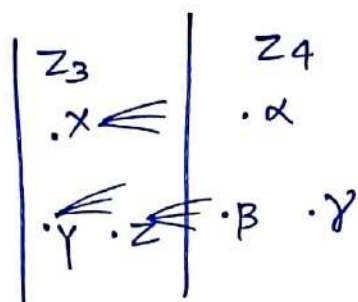
$\frac{1}{Th=4} \times \frac{3}{2 \text{ or } 3 \text{ or } 4} \times \frac{3}{2 \text{ or } 3 \text{ or } 4} \times \frac{3}{2 \text{ or } 3 \text{ or } 4} = 27$
 $- 1 (4222) \rightarrow \text{invalid}$
 Total no. = 54 - 3 = 51 no's Ans
 (valid)



Now

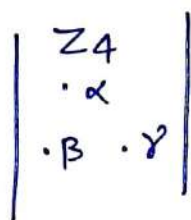


Now



Total = 90 Ans ∴

Now



Q> 10 identical Balls are to be distributed among 3 friends. In how many ways can the distribution be done?

Sol> whole no. soln.

$a + b + c = 10$

+ 11

$$a + b + c = 10$$

$$\begin{array}{r} 1 \quad 9 \quad 9 \\ 2 \quad 8 \quad 8 \\ \vdots \quad \vdots \quad \vdots \\ 9 \quad 0 \quad 0 \end{array} \left. \vphantom{\begin{array}{r} 1 \\ 2 \\ \vdots \\ 9 \end{array}} \right\} \rightarrow 10$$

$$\begin{array}{r} 2 \quad 8 \quad 7 \\ 8 \quad 0 \quad 0 \end{array} \left. \vphantom{\begin{array}{r} 2 \\ 8 \end{array}} \right\} \rightarrow 9$$

$$\begin{array}{r} 9 \quad 0 \quad 1 \\ 0 \quad 1 \quad 0 \end{array} \left. \vphantom{\begin{array}{r} 9 \\ 0 \end{array}} \right\} \rightarrow 2$$

$$\begin{array}{r} 10 \quad 0 \quad 0 \end{array} \left. \vphantom{\begin{array}{r} 10 \end{array}} \right\} \rightarrow 1$$

$$11 + 10 + 9 + 8 + 7 + 6 + 5 + 4 + 3 + 2 + 1 = 66$$

$$(or) \frac{11 \times 12}{2} = 66 \checkmark$$

$$\frac{n(n+1)}{2}$$

Shortcut CONDITIONAL
soln.

N. No. soln

$$a + b + c = 10$$

$$\uparrow \quad \uparrow \quad \uparrow$$

whole No. soln. ($\because$ 1 Ball all have)
 $A + B + C = 7$

hence,

$$7 + 3 - 1 \quad C_{3-1}$$

$${}^9C_2 = \frac{9 \times 8}{2} = 36 \checkmark \text{ Ans.}$$

0 Balls can be possibly assigned to anyone

Shortcut

$${}^{(n+r-1)}C_{(r-1)}$$

① $n \rightarrow$ identical objects

② whole no. soln.

applicable

whole no. soln. $\rightarrow$ means can give 0 ball also.

$n \rightarrow$ identical objects

$r \rightarrow$ no. of people.

$$\text{here sol } (10 + 3 - 1) C_{(3-1)}$$

$$= {}^{12}C_2 = \frac{12 \times 11}{2} = 66.$$

Now

Natural No. soln.

$$a + b + c = 10$$

$$\begin{array}{r} 1 \quad 1 \quad 8 \\ 2 \quad 7 \quad 1 \\ \vdots \quad \vdots \quad \vdots \\ 8 \quad 1 \quad 1 \end{array} \left. \vphantom{\begin{array}{r} 1 \\ 2 \\ \vdots \\ 8 \end{array}} \right\} \rightarrow 8$$

$$\begin{array}{r} 2 \quad 1 \quad 7 \\ 2 \quad 6 \quad 1 \\ \vdots \quad \vdots \quad \vdots \\ 7 \quad 1 \quad 1 \end{array} \left. \vphantom{\begin{array}{r} 2 \\ 2 \\ \vdots \\ 7 \end{array}} \right\} \rightarrow 7$$

$$\frac{8 \times 9}{2} = 36$$

$$\begin{array}{r} 7 \quad 1 \quad 2 \\ 8 \quad 1 \quad 1 \end{array} \left. \vphantom{\begin{array}{r} 7 \\ 8 \end{array}} \right\} \rightarrow 2$$

Noneed

$$\therefore {}^nC_2 = \frac{n(n-1)}{2}$$

Q 15 identical Balls are to be distributed among 4 friends (A, B, C, D) such that A should get atleast 3 balls, B atleast 2, C atleast 1. In how many ways can the distribution be done

Sol

$$\begin{matrix} A & + & B & + & C & + & D & = & 15 \\ 3 & \rightarrow & 2 & \rightarrow & 1 & \rightarrow & 0 \end{matrix}$$

$$15 - 6 = 9$$

$$A + B + C + D = 9$$

$$\begin{aligned} 9 + 4 - 1 C_{4-1} &= {}^{12}C_3 = \frac{12!}{3!9!} = \frac{12 \times 11 \times 10 \times 9!}{9! \times 3!} \\ &= \frac{12 \times 11 \times 10}{6} \\ &= 220 \end{aligned}$$

* GEOMETRICAL P and C :-

12 points
~~ooooo~~

st. lines

$${}^{12}C_2 \text{ (if no points are collinear)} - {}^5C_2 \text{ (5 points are collinear)} + 1 \text{ (one line possible)}$$

$n C_2$

12 points
~~ooooo~~

Δ 's

$${}^{12}C_3 \text{ (if no points are collinear)} - {}^5C_3 \text{ (5 points collinearity)}$$

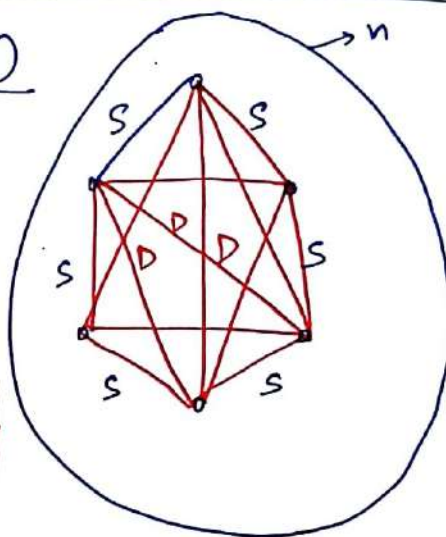
$n C_3$

No. of diagonals of any 'n' sides polygon = $\frac{n(n-3)}{2}$

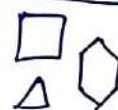
$n C_2 = \text{All sides} + \text{All Diag}$

any 2 vertex makes handshake
↓
side, Diagonal

$$\left\{ \begin{aligned} n C_2 - n &= \text{All diagonals} \\ \frac{n(n-1)}{2} - n &= \frac{n(n-3)}{2} \end{aligned} \right\}$$



Polygon
n sides
↑
n vertex



Q> If no. of diagonals of a n sided polygon is 50% more than its no. of sides then the polygon is —

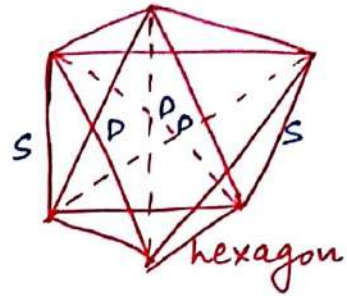
Sol $\therefore 1.5x = \frac{x(n-3)}{2}$

$n-3 = 3$

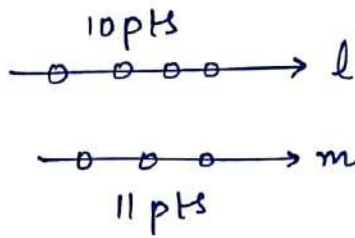
$n=6$

→ sides, 9 diagonals

$\begin{matrix} S & D \\ \downarrow & \downarrow \\ 6 & 9 \end{matrix}$



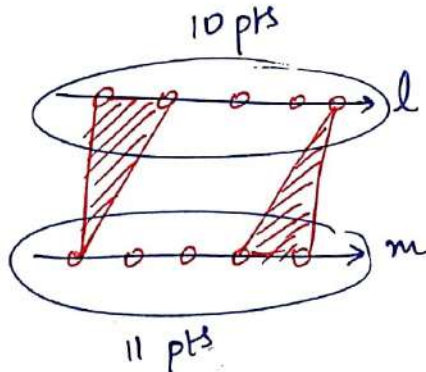
Q>
211m



how many Δ 's can we get from these 21 pts.

Sol ${}^{21}C_3 - {}^{10}C_3 - {}^{11}C_3$
 $1330 - 1 - 1$

SIR



$\frac{{}^{11}C_2 \times 10}{} + \frac{{}^{10}C_2 \times 11}{} = 550 + 445 = 1045 \checkmark$

${}^{21}C_3 - {}^{10}C_3 - {}^{11}C_3 = 1045 \checkmark$

{ all 3 should not from the same line }

Chess Board

$$n+1C_2 \rightarrow n+1C_2 = \left[\frac{(n+1)n}{2} \right]^2$$

$$nC_2 = \frac{n(n-1)}{2}$$

$$9C_2 \times 9C_2 = 1296 \text{ Rectangles}$$

$$204 \text{ Squares}$$

$$\sum n^3 = \left[\frac{n(n+1)}{2} \right]^2 = 1296$$

1) Rectangles (n x n)

2) Squares

3) different types of Rectangles

$$204$$

$$\sum n^2 = \frac{n(n+1)(2n+1)}{2} = 204$$

put $n=8$

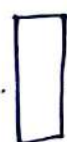
$$\sum n = \frac{n(n+1)}{2} = 36$$

put $n=8$

1	
2	
3	
4	

area & perimeter same $\rightarrow$ then same type

orientation diff.



4x1

4x1

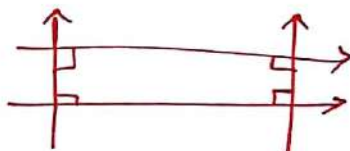
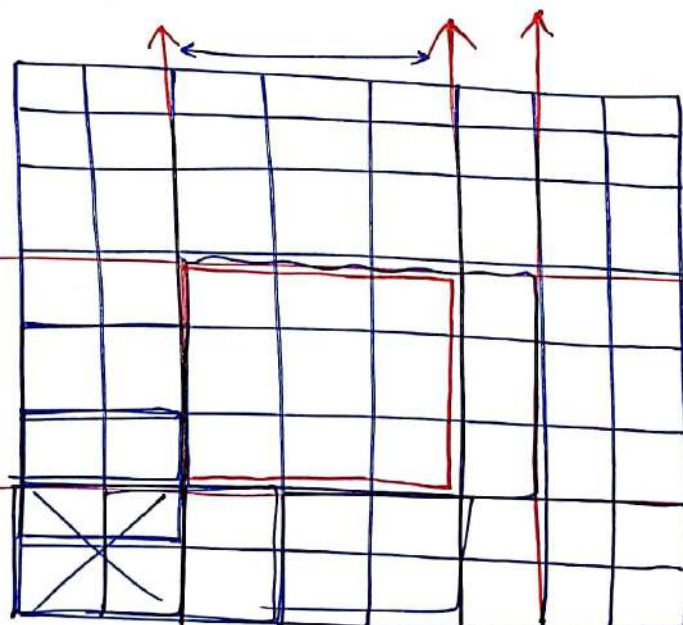
$$P=10$$

$$P=10$$

$$A=4$$

$$A=10$$

hence same Rectangle.



$$1 \times 1 \rightarrow 64 \rightarrow 8^2$$

$$2 \times 2 \rightarrow 7^2 \rightarrow 49$$

$$3 \times 3 \rightarrow 8^2 \rightarrow 36$$

$$\vdots$$

$$7 \times 7 \rightarrow 4 \rightarrow 2^2$$

$$8 \times 8 \rightarrow 1 \rightarrow 1^2$$

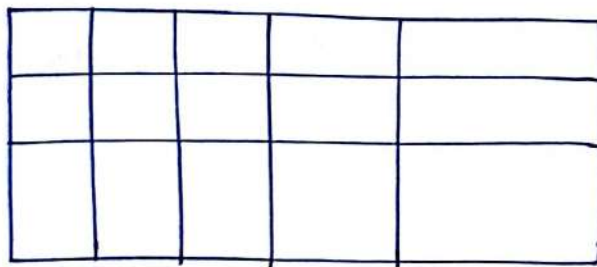
$$204$$

$1 \times 1, 1 \times 2, 1 \times 3, \dots, 1 \times 8 \rightarrow 8 \text{ types}$
 $2 \times 2, 2 \times 3, 2 \times 4, \dots, 2 \times 8 \rightarrow 7 \text{ types}$
 $3 \times 1, 3 \times 2, 3 \times 3, 3 \times 4, 3 \times 5, \dots, 3 \times 8 \rightarrow 6 \text{ types}$
 $\vdots$
 $8 \times 8 \rightarrow 1 \text{ type}$

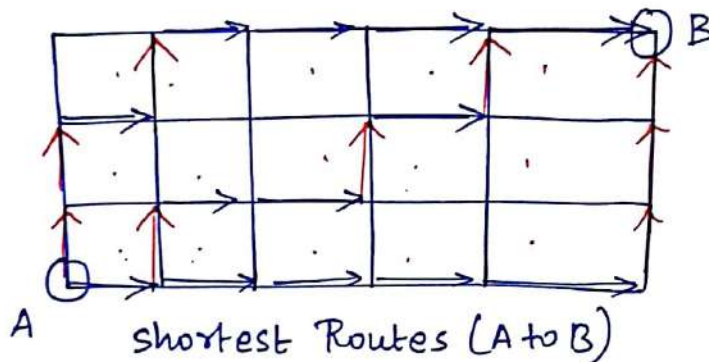
all squares are included (जाने दो)

36

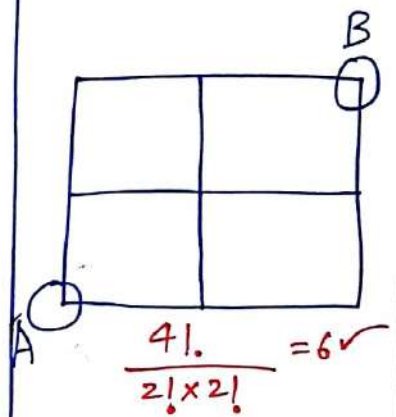
Gate 2017
2 marks



Redraw



CSAT (2011)



how many shortest routes are possible b/w A & B?

Sol

$$\frac{(R+C)!}{R! \times C!} = \frac{(5+3)!}{5! \times 3!} = 56.$$

Ex:- Apple = $\frac{5!}{2!} = 60$

BANANA = $\frac{6!}{3! \times 2!}$

[HHHHH VVV] = $\frac{8!}{5! \times 3!} = 56$

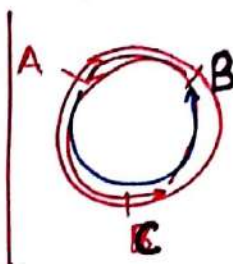
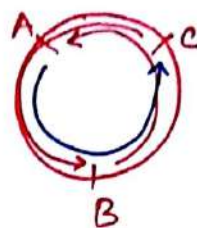
{H V H V H V H H}

* Linear Arrangement / Permutation :-

$$3 \times 2 \times 1 = 3! \quad (n!) \\ \text{---} \quad \text{---} \quad \text{---} \\ \left. \begin{array}{l} \{ a \ b \ c \} \\ \{ a \ c \ b \} \\ \{ b \ c \ a \} \\ \{ b \ a \ c \} \\ \{ c \ a \ b \} \\ \{ c \ b \ a \} \end{array} \right\} 6 \text{ ways}$$

circular Pn / circular arrangement.

$$(n-1)! \\ (3-1)! = 2! \quad (2 \text{ ways})$$



Q> A couple invited their 10 friends to a dinner party ^{to be held} across a circular dinning table having 12 chairs such that there ~~has to~~ have to be exactly 1 friend b/w the couple.

Sol

$$\frac{8!}{\cancel{8!}}$$

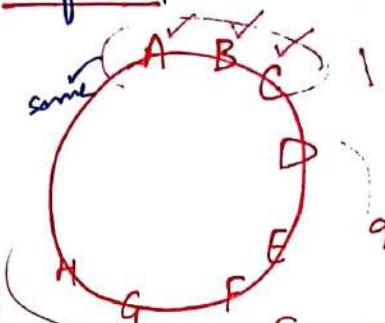
SIR



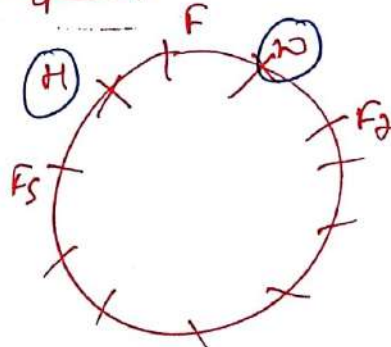
$$2! (10 \times 9!)$$

$$2! \times 10!$$

$$2 \times 10! \quad \text{Ans}$$



H, W can interchange



Q> all 5 digit natural No's are being formed from 1st five natural no's without repetition. what is ^{sum} ~~sum~~ of all of those no's

$$(n-1)! \times \underbrace{11111}_{\text{n times}} (\sum d)^{\text{digits}}$$

$$(5-1)! \times 11111 (1+2+3+4+5)$$

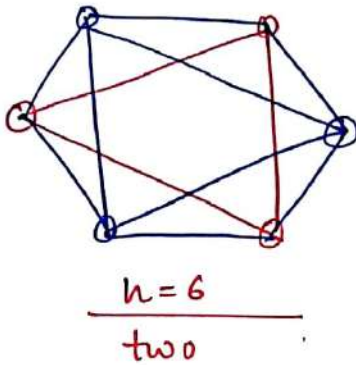
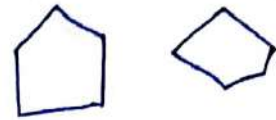
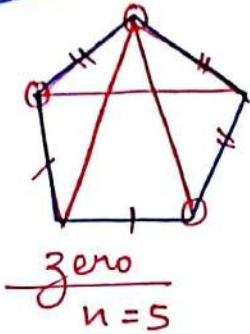
$$4! \times 11111 \times 15$$

CAT 2009

1, 3, 5, 7, 9

Q> vertex of a octagon are joined and Δ s are formed. How many Δ s are there whose vertex belongs to the vertex of octagon but none of its sides should belong to the side of octagon?

Sol SIR



me ✓

$$n=6$$

$$\Delta = \frac{n(n-5)}{3}$$

$$\frac{6 \times 1}{3} = 2$$

$$\frac{8 \times 2}{3} = \frac{16}{3}$$

$$\frac{8(3)}{3} = 8$$

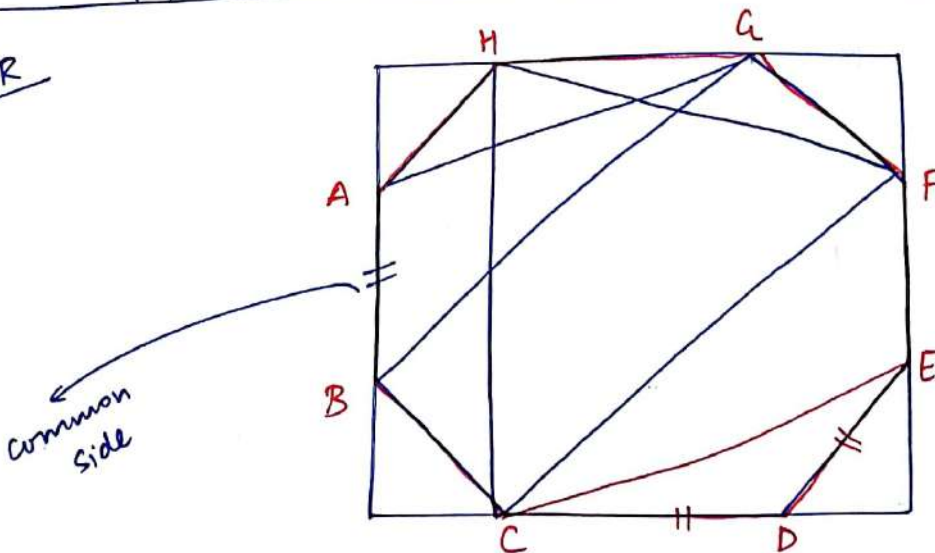
$$\frac{5 \times 2}{3} = \frac{10}{3}$$

$$\frac{11}{11}$$

$8(3) \times$

$$\left. \begin{array}{l} n^2 - (n^2 - 2) \\ 36 - 34 \\ 2 \end{array} \right\} \begin{array}{l} 0 \downarrow 6 \\ 5 \downarrow 2 \end{array}$$

SIR



$$T(\Delta) \Rightarrow {}^8C_3$$

(no 3 collinear)

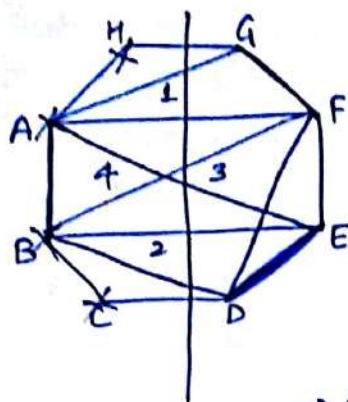
$$T(\Delta) = \Delta(1)$$

common side

$$+ \Delta(2) (CDE)$$

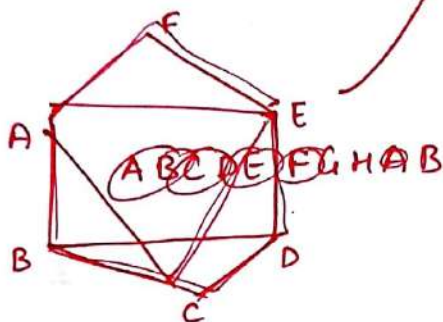
$$+ \Delta(0) \rightarrow HCF$$

$$8C_3 = \Delta(1) + \Delta(2) + \frac{\Delta(0)}{?}$$



AB gone
HC also

AB side $\rightarrow 4\Delta$
8 side $\rightarrow 8 \times 4\Delta$



$$T(\Delta) = \Delta(1) + \Delta(2) + (\Delta(0)?)$$

$$n(3) = (4\Delta \times 8) + \binom{n}{8} + \Delta(0)$$

$$56 = 32 + 8 + \Delta(0)$$

$$\Delta(0) = 16$$

0 side common

$$n(3) = n(n-4) + n + \Delta(0)$$

4 points
gone

$$\Delta(0) = n(3) - n(n-4+1)$$

02/10/2016

PROBABILITY

Classical Defⁿ:-

$$P = \frac{\text{favourable chances}}{\text{Total chances}} = \text{Probability}$$

Sample space = $\{1, 2, 3, 4, 5, 6\}$
in case of a dice

SS = $\{H, T\}$
in case of a coin

unbiased Events $\rightarrow$ every event (equally likely)

$$P(1) = \frac{1}{6}$$

$$P(2) = \frac{1}{6}$$

$$P(3) = \frac{1}{6}$$

$$\vdots$$

$$P(6) = \frac{1}{6}$$

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

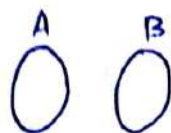
Mutually exclusive events

and

Independent Events

{ Next Page }

✓ Mutually Exclusive events are events where happening of one event guarantees non-happening of the other.
means $A \rightarrow \text{happen}, B \rightarrow \text{not happen}$.



$A, B \rightarrow \text{disjoint sets}$

$$P(A \cap B) = 0$$

for M.E.E.

Additive Rule

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

only one of the events happen @ time.

$$P(A \cup B \cup C) = P(A) + P(B) + P(C)$$

“oh”

English identifying key-word.

Q → Dice

$$P(\text{even}) + P(\text{odd}) - P(\text{even and odd}) = P(\text{even oh odd})$$

$$= \frac{3}{6} + \frac{3}{6} - 0 = P(\text{even})$$

✓ Independent Events are Events where more than one event can happen at a time without influencing the result of each other.

Ex:- Coin and dice is tossed simultaneously.

“and”

hint (1).

Product Rule

$P(3m)$ and $P(t)$
multiply
tossed → (tail)

$$\frac{2}{6} \times \frac{1}{2} = \frac{1}{6}$$

$$P(A) \times P(B) \times P(C)$$

Q → $P(A) = 60\%$ → A speaks Truth in 60% cases.

$P(B) = 75\%$

while answering the same qn. in either “Yes” or “No” they are likely to fight with each other in what % chances.

Sol:-

$$P(A) = \frac{3}{5}, P(\bar{A}) = \frac{2}{5}$$

$$P(B) = \frac{3}{4}, P(\bar{B}) = \frac{1}{4}$$

mutually exclusive

$$A \times \bar{B} + B \times \bar{A}$$

$$\frac{3}{5} \times \frac{1}{4} + \frac{3}{4} \times \frac{2}{5}$$

$$= \frac{9}{20} \approx \frac{45}{100} \approx 45\%$$

Q> There are 2 vacancies for which the husband and wife applied, $P(h) = 1/7 \rightarrow$ Probability of husband gets the job.
 $P(w) = 1/5$

only one gets the job	both	None	atleast one
?	?	?	?

Q> x is randomly chosen from 1st 100 natural no., what is the probability that chosen x satisfies the inequality

a) $\frac{28}{50}$

$$\frac{(x-40)(x-70)}{(x-30)} < 0$$

b) $\frac{29}{50}$

$$x \in [0, 100]$$

c) $\frac{59}{100}$

d) $30/50$

Q> A and B decided to meet b/w 6 and 7 p.m. on 14th Febr. 2017. what is the probability that they will meet provided one cannot wait for other for more than 20 minutes?

Q> Gate Qⁿ.

Sol> ① $P(h) = 1/7$ $P(\bar{h}) = 6/7$
 $P(w) = 1/5$ $P(\bar{w}) = 4/5$

$$\left(\frac{1}{7} \times \frac{4}{5}\right) + \left(\frac{6}{7} \times \frac{1}{5}\right)$$

$$4/35 + 6/35$$

$$10/35$$

$$0.28$$

$$\frac{10}{35}$$

0.02
0.68

③ 1 hr 20 min $\frac{5}{9}$
 0.33×0.33
 0.66
 $0.25 \times \rightarrow 0.0625$

② $x - 40 < 0$ $\frac{29}{50}$ ✓
 $x < 40, x < 70$
 $x < 30$

40% 70%
 $\sqrt{30\%}$

0 100
 101 98
 3 101
 0.97

④ $\rightarrow$ Gate $\frac{7}{16}$

SIR (1) $P(h) = 1/7$, $P(\bar{h}) = 6/7$
 $P(w) = 1/5$, $P(\bar{w}) = 4/5$

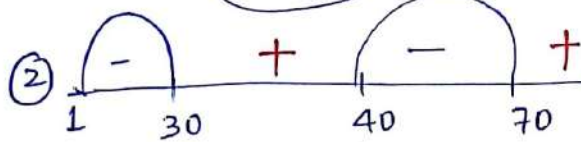
only one	both	none	@ least one
$h \times \bar{w} + \bar{h} \times w$ $1/7 \times 4/5 + 1/5 \times 6/7$ $\frac{10}{35}$	$h \times w$ $1/7 \times 1/5$ $\frac{1}{35}$	$\bar{h} \times \bar{w}$ $6/7 \times 4/5$ $\frac{24}{35}$	

1 = only one + both + None

1 = $\frac{10}{35} + \frac{1}{35} + \frac{24}{35}$

$\downarrow$
 $\frac{11}{35} \leftarrow P(\text{@ least one})$

$1 - \frac{24}{35}$

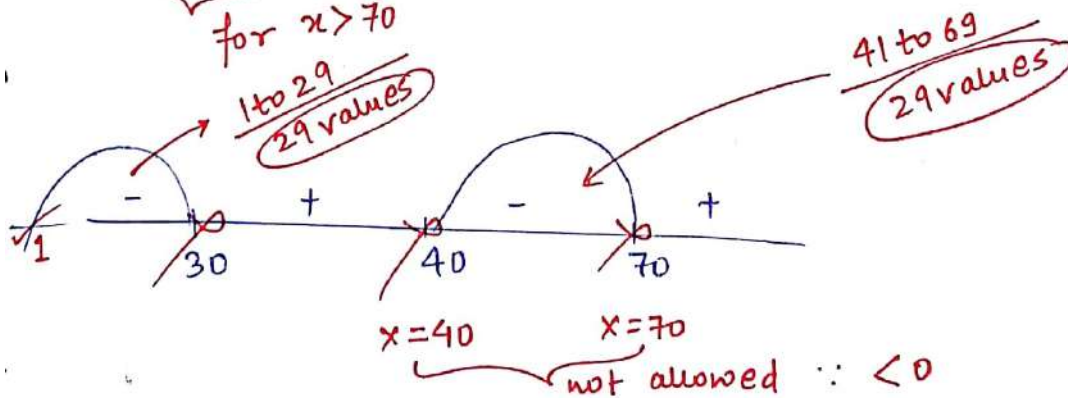


$\frac{(x-40)(x-70)}{(x-30)} < 0$

for $x > 70$

similarity

signs can be putted on the no. line in alternate fashion.

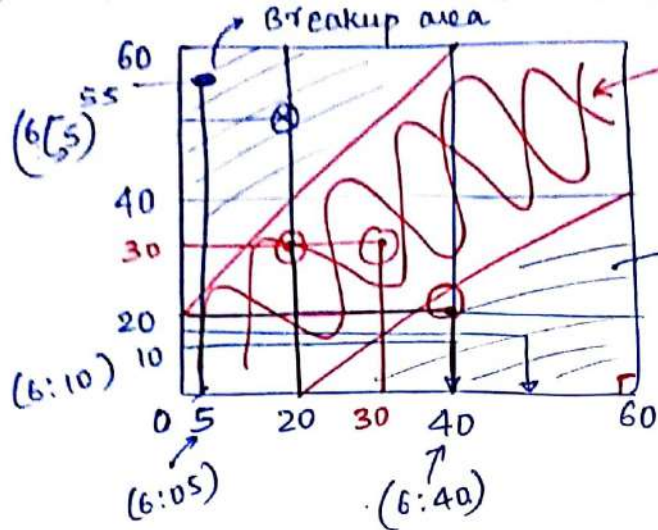


$\frac{\text{fav. chances}}{\text{Total chances}} = \frac{58}{100} = \frac{29}{50}$

(3) Time $\rightarrow$ Real No.

∞ no. of values b/w 6 & 7.

$\frac{\text{favourable chances}}{\text{Total chances}} = \frac{\infty}{\infty} = \frac{f(A)}{T(A)}$
 favourable area / Total area



6:20 - 6:40 → Just a moment.

here, $\Delta = \frac{1}{2} \times 40 \times 20 = 800 \text{ units}$

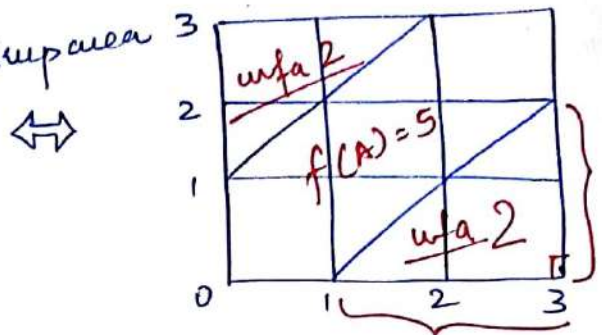
unfav Area = 1600 units.

Total area $TA = 60 \times 60 = 3600$

favourable area $fA = 3600 - (800 \times 2) = 2000$

$$\frac{f(A)}{T(A)} = \frac{2000}{60 \times 60} = \frac{20}{36}$$

$$TA = 9$$



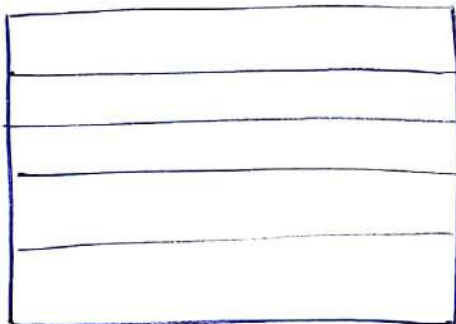
area $(\Delta) = \frac{1}{2} \times 2 \times 2 = 2 \text{ units}$

unfavourable area = $2 \times 2 = 4 \text{ units}$

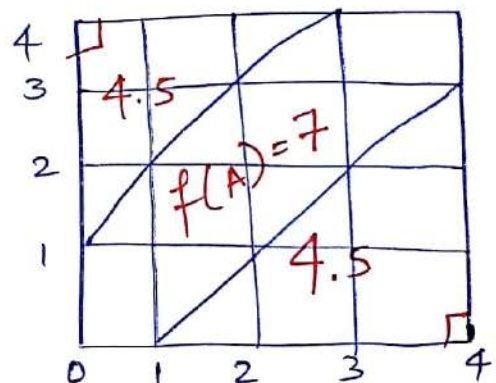
favourable area = $9 - 4 = 5 \text{ units}$

hence, $\frac{f(A)}{T(A)} = \frac{5}{9}$

④



Red row



$$\frac{f(A)}{TA} = \frac{7}{16}$$

Conclusion

if $TA \rightarrow \frac{(TA) - (unfav)}{3 \times 3} = \frac{5}{9}$

formulae

$$\frac{(2n-1)}{n^2}$$

Ans:

if $TA \rightarrow \frac{4 \times 4 - 3 \times 3}{4 \times 4} = \frac{7}{16}$

$$\frac{6 \times 6 - 5 \times 5}{6 \times 6} = \frac{11}{36}$$

Maths behind it

$$\left. \begin{array}{l} 0 \leq x \leq 60 \\ 0 \leq y \leq 60 \end{array} \right\} TA$$

$$|x-y| \leq 20 \} f(A)$$

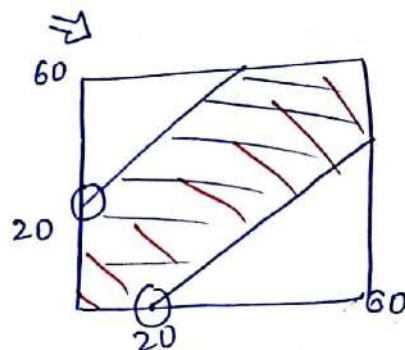
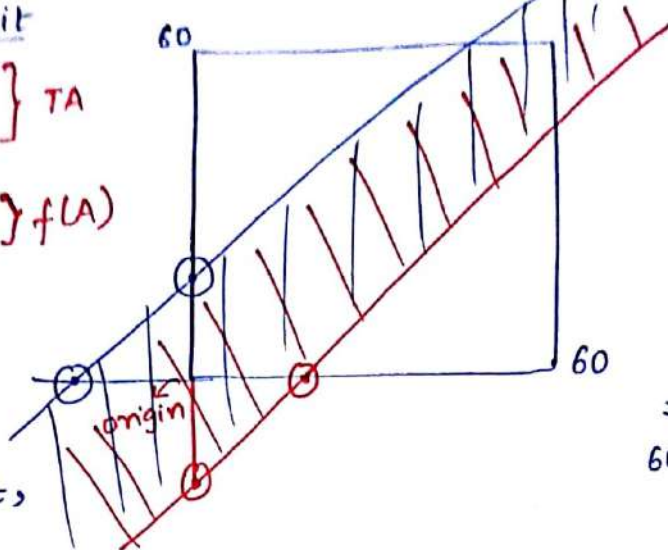
$$x-y = 20$$

if $x-y \leq 20$

if y comes first,

$$y-x = 20$$

$y-x \leq 20 \rightarrow$ To satisfy this ⁱⁿ equality, we have to move towards origin.



Do $\rightarrow$ (33) (41) Pg 72

(33) 1 - - - - - 100

2 digit integers

not divisible by 7

$$7 \times 7 = 49$$

~~7~~, ~~14~~, ~~21~~, ~~28~~, ~~35~~, ~~42~~, ~~49~~, ~~56~~, ~~63~~, ~~70~~,
~~77~~, ~~84~~, ~~91~~, ~~98~~

(14) no.

10

10 - - - 100

$$\begin{array}{r} \textcircled{91} \\ - 14 \\ \hline 77 \end{array}$$

SIR [1-100] $\div$ by 7

$$\frac{100}{7} = 14 \quad [\cancel{7}, 14, 21, \dots, 98]$$

[10-99] $\rightarrow$ Total No.'s = (90)

$$\text{div. by } 7 \Rightarrow (14-1) = (13)$$

$$\frac{fC}{TC} = \frac{77}{90} \checkmark$$

Q2) $11Y = 366d = (52 \times 7) + 2 \text{ odd day}$ → 2 chances of Saturday

53rd Saturday

$\frac{fc}{TC} = \frac{2}{7}$ ✓
 FS
 SS
 SM
 MT
 TW
 WT
 TF

7

Ans: $\frac{2}{7}$

* Sample space (dice) = $\{1, 2, 3, \dots, 6\}$

$P(\text{even}) = \frac{3}{6} \rightarrow \{2, 4, 6\}$

$P(\text{prime}) = \frac{3}{6} \rightarrow \{2, 3, 5\}$

Q3 (Conditional Probability Based).

A dice is thrown at random. What is the probability of getting a prime no. on the dice provided the dice had shown an even number.
↓ already shown.

Sol: $SS_{\text{new}} = [2, 4, 6]$

$P(\text{prime}) = P\left(\frac{\text{prime}}{\text{even}}\right) = \frac{1}{3}$ ✓

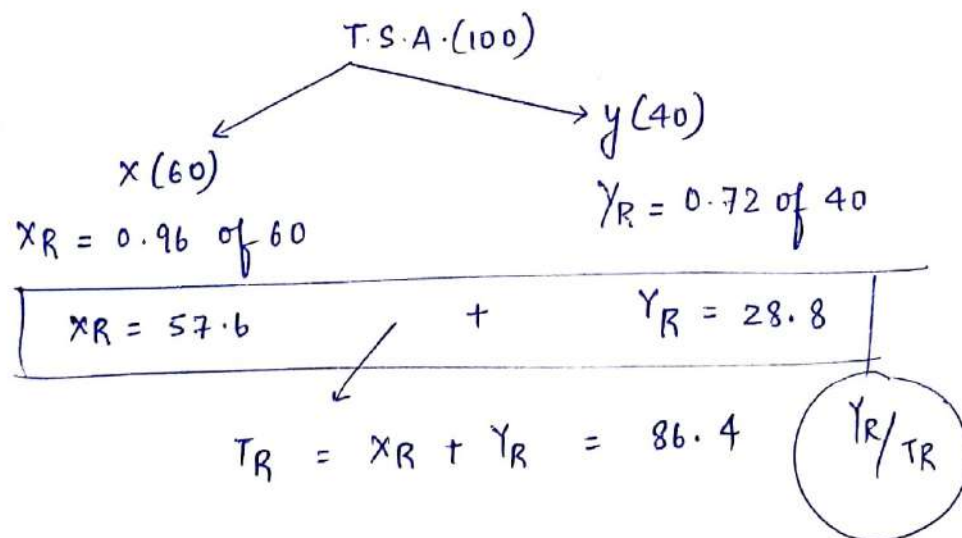
Pg 71 (20) X, Y

$X \rightarrow 60\% \rightarrow 96\% \text{ reliable}$

$Y \rightarrow 40\% \rightarrow 72\% \text{ reliable}$

96/100

0.576 0.288



(53)

$$\frac{10}{100} \rightarrow \text{HIV}^+$$

$$\text{HIV}^+ \rightarrow 95\% \text{ (True)}$$

$$\text{HIV}^- \rightarrow 89\% \text{ (-" -)}$$

SIR

$$\frac{0.1 \times 0.95}{(0.1 \times 0.95) + (0.9 \times 0.11)}$$

$\uparrow \quad \uparrow \quad \quad \uparrow \quad \uparrow$
 +ve +ve -ve m/c $\rightarrow$ +ve
 (-vector)

0.4896

 Ans

Pg 54

$$(5) P(2) = 1$$

$$P(3) = 2$$

$$P(4) = 3$$

$$P(5) = 4$$

$$P(6) = 5$$

$$P(7) = 6$$

$$P(8) = 5$$

$$P(9) = 4$$

$$P(10) = 3$$

$$P(11) = 2$$

$$P(12) = 1$$

Pg 54

$$(6) \frac{1}{3} \times \frac{1}{4} \times \frac{1}{5} \times \frac{1}{6}$$

independent events

SIR

None of them solves qn.

$$\bar{A} \times \bar{B} \times \bar{C} \times \bar{D}$$

Qn is not solved

$$Qn. \text{ is solved} \Rightarrow 1 - (\bar{A} \times \bar{B} \times \bar{C} \times \bar{D})$$

 (or) atleast one of them solves Question

 All of them solves the Qn. $\Rightarrow A \times B \times C \times D$

Q7

4 times

2H, 2T

HHHT	HHTH	HTHH	THHH
HHTT	HTHT	HTTH	THTH
HHTT	THHT	TTHT	TTTH
TTTT	HHHH		

$\cancel{4/16} \quad \frac{1}{4}$

H	H	T	T
H	T	H	T
H	T	T	H
T	H	H	T
T	H	T	H
T	T	H	H

$$\frac{6}{16} \rightarrow \text{alter.}$$

$$\text{alter. method} \rightarrow {}^4C_2 \left(\frac{1}{2}\right)^2 {}^2C_2 \left(\frac{1}{2}\right)^2$$

$\frac{6}{16}$

Q 10 penalty shootouts. ${}^{10}C_4 \rightarrow$ chances in which goal happens.

$$\frac{4!}{0!4!}$$

$({}^{10}C_4 \cdot (\frac{8}{9})^4)$ success ${}^6C_6 (\frac{1}{9})^6$

Pg 90
 (1.77)

${}^{10}C_6 \times$

0.2508

Pg 54
 $(10) \frac{0.04}{100} = (\frac{1}{25})$

Pg 54
① $nC_2 = n \cdot \text{shakes}$

$\frac{n(n-1)}{2} = 153$

①8 ✓

② ✓

* LOGICAL REASONING ✓

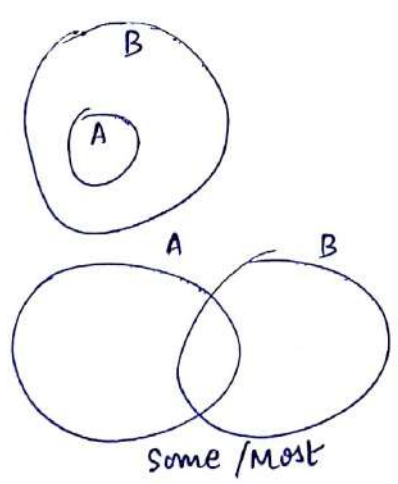
4 Rules $\rightarrow$ Rule 1 $\rightarrow$ draw all possibilities/(Cases).

Rule 2 $\rightarrow$ for a statement to be True, it have to be true in all the cases.

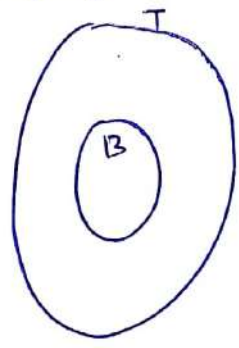
Rule 3 $\rightarrow$ If a statement is false even in one of the case, then it will be considered false forever.

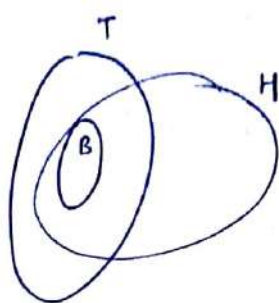
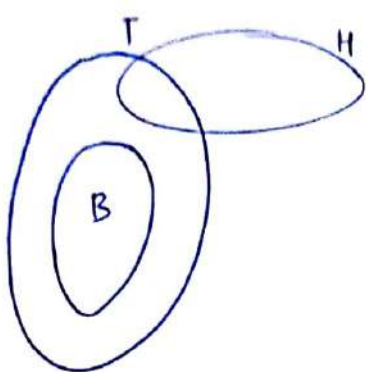
Rule 4 $\rightarrow$ Try to proof a statement false as early as possible.

Rules/General $\rightarrow$ Read dirn's carefully ↑



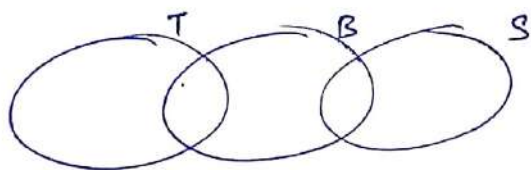
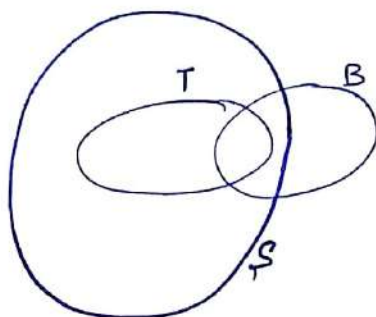
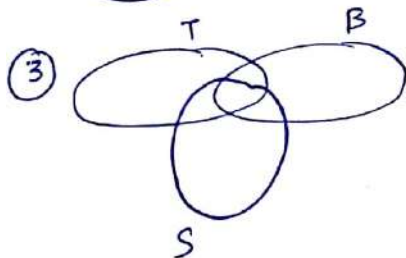
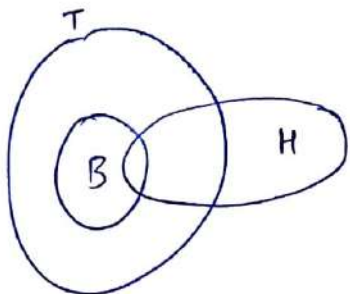
Q2



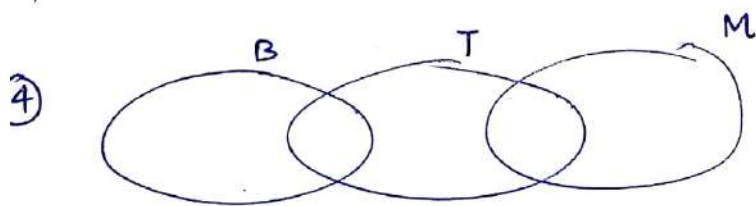


no informn. about
news and Birds
hence
3 possibilities.

conc i ~~x~~
ii ~~x~~ (b)

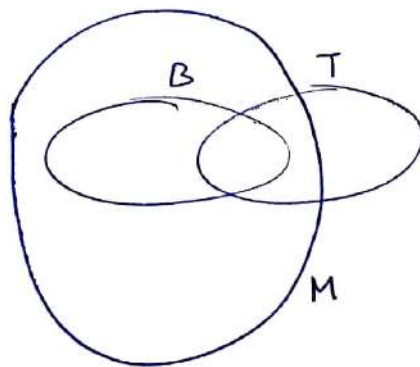
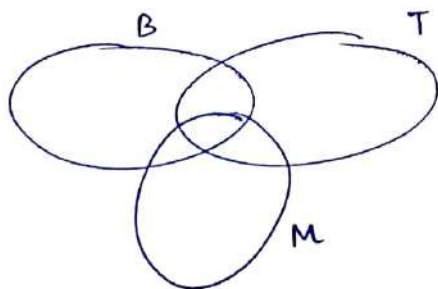


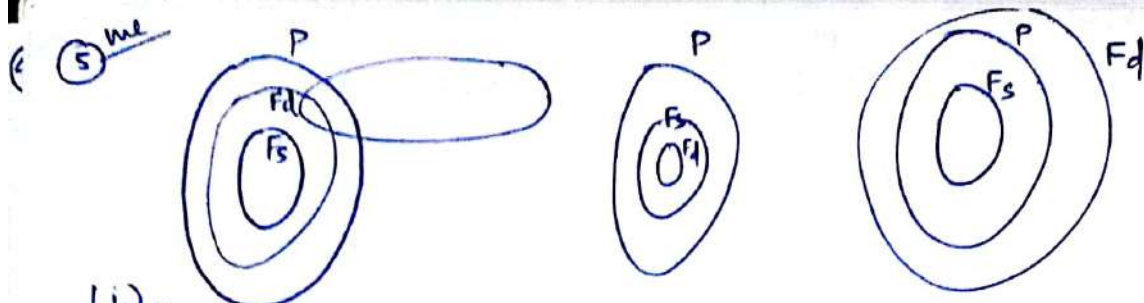
i. ~~x~~
ii ~~x~~ (a) ✓



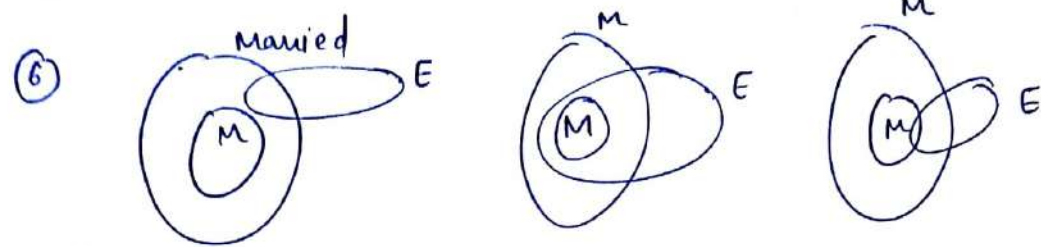
(i.) ~~x~~
(ii.) ~~x~~

(d) ✓

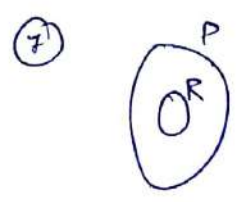




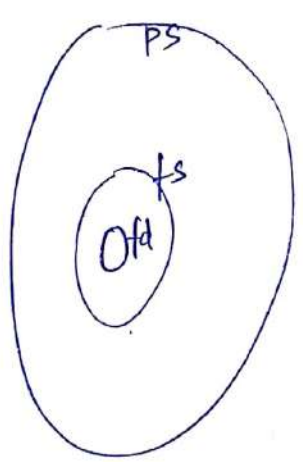
(i) x
(ii) ✓ (b) ✓



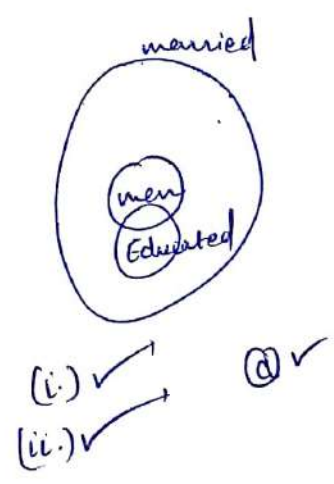
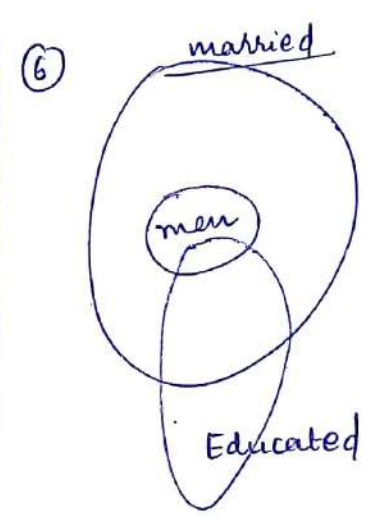
(i) ✓
(ii) ✓ (c)



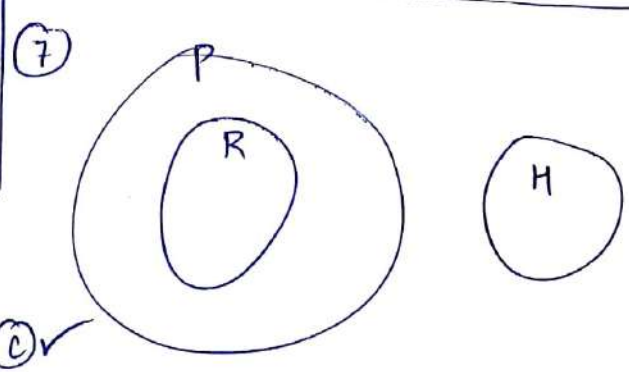
SIR
(5)



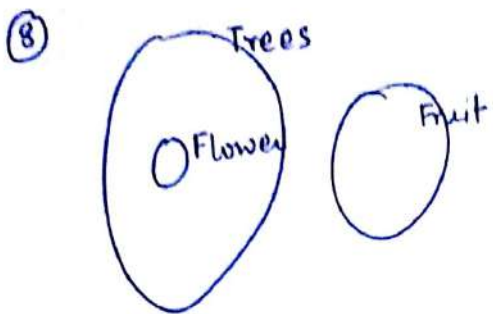
i ✓
ii ✓ (d) ✓



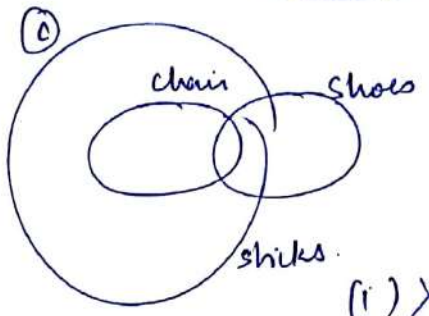
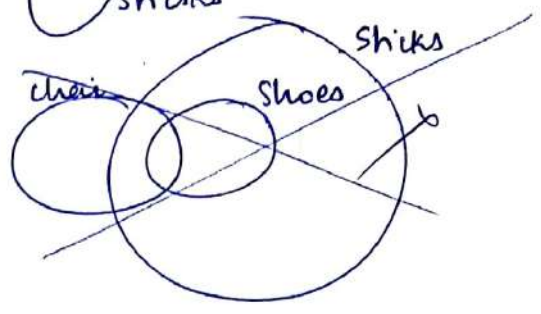
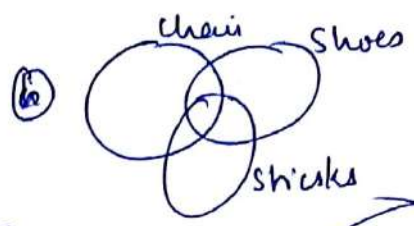
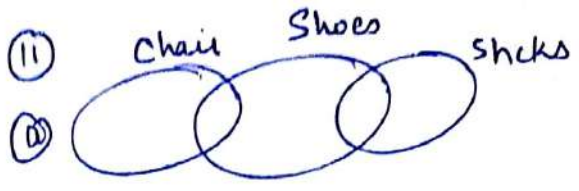
(i) ✓
(ii) ✓ (d) ✓



(1) x
(2) x (c) ✓



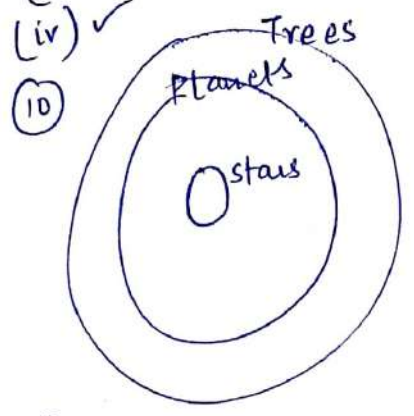
- ① ✓
- ② ✓
- ④ ✓



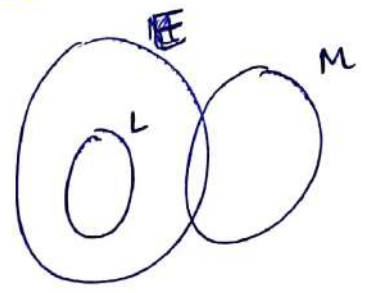
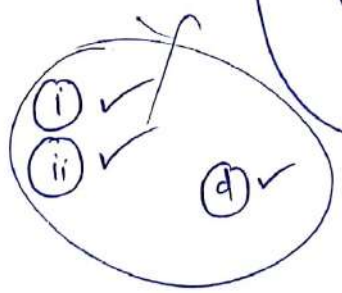
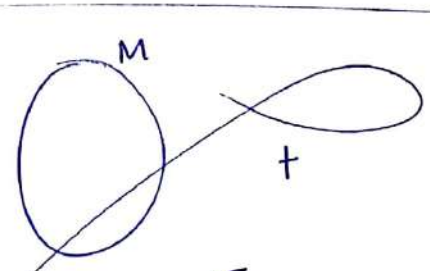
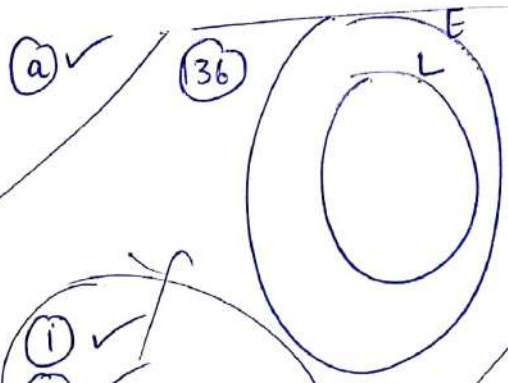
- (i) ✗
- (ii) ✗
- (iii) ✗
- (iv) ✗
- ④ ✓



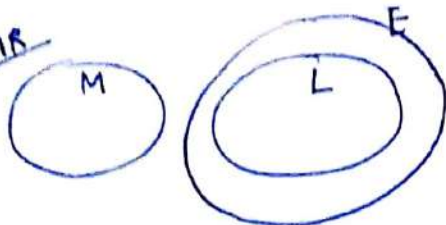
- (i) ✗
- (ii) ✗
- (iii) ✓
- (iv) ✓
- ③ ✓



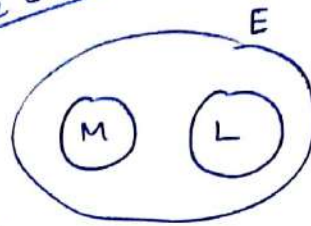
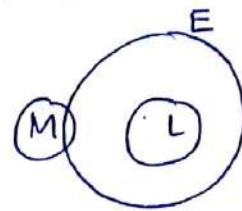
- (i) ✗
- (ii) ✓
- (iii) ✗
- (iv) ✓



Q 136 SIR



No informⁿ about Manager and Executive



hence Cases

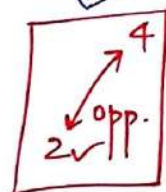
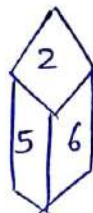
(i) ✗ (Bullshit)

(ii) ✗ —

(c) ✓

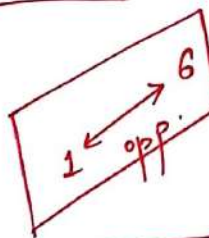
Pg no. 57

8 to 9



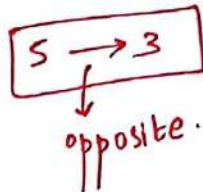
4 opposite 1, 2, 3, 5, 6
5 opposite 1, 2, 3, 4, 6
1 opposite 2, 3, 4, 5, 6

∴ all are adjacent



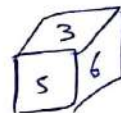
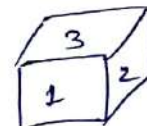
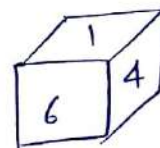
6 opposite 1, 2, 3, 4, 5

5 opposite 1, 2, 3, 4, 6



Q 137

1, 2, 3, 4, 5, 6

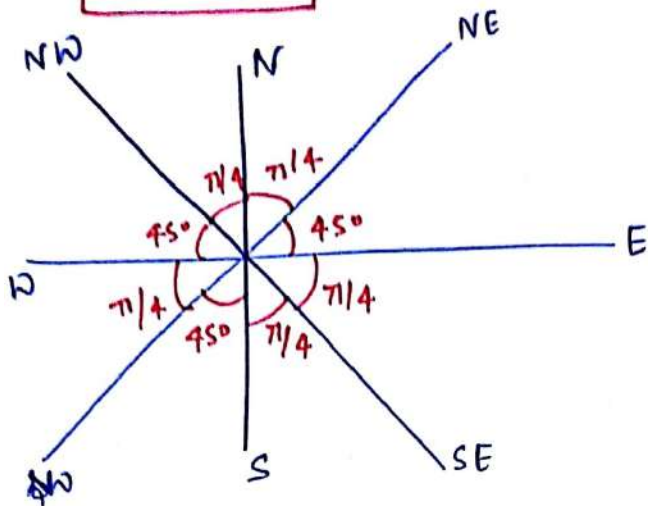


1 opposite 2, 3, 4, 5, 6

1 opposite 5

(a) ✓

* DIRECTION :-



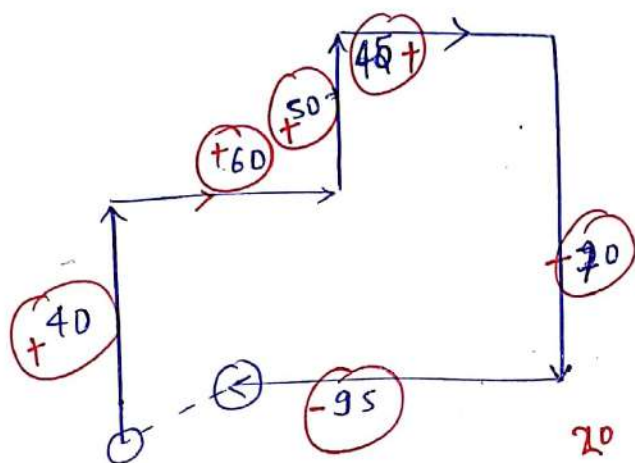
Horizontal ^(H) = E^+, W^-

Vertical ^(V) = N^+, S^-

Apply pythagoras.

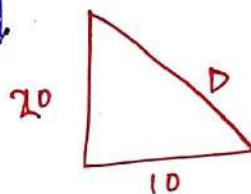
$$D = \sqrt{H^2 + V^2}$$

Q. Person goes 40m North take a Right turn goes 60m takes a left Turn ^{goes} 50m and takes another " " " 45m



$$H = |60 + 45 - 95| = 10$$

$$V = |40 + 50 - 70| = 20$$

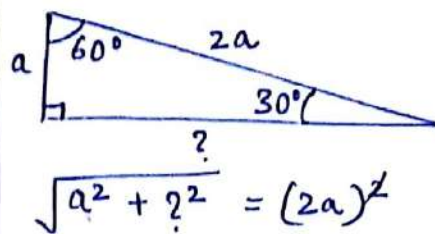
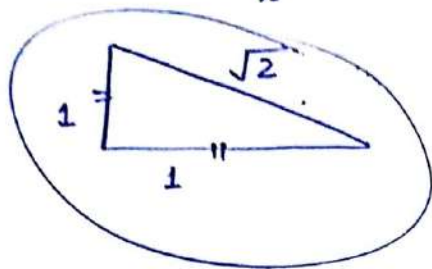
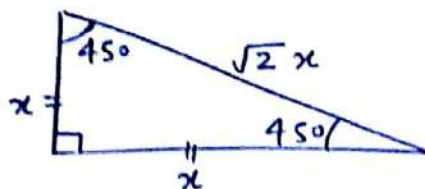


$$D = \sqrt{10^2 + 20^2}$$

$$D = \sqrt{500}$$

$$D = 10\sqrt{5} \text{ Ans}$$

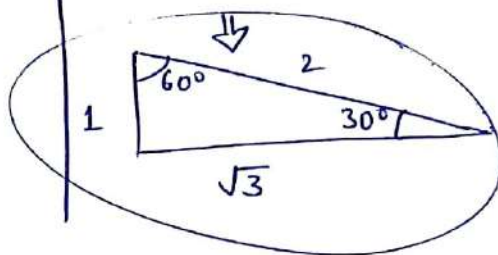
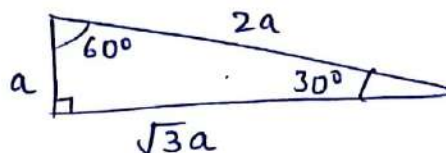
Isosceles Right $\triangle$



$$\sqrt{a^2 + ?^2} = (2a)^2$$

$$a^2 + ? = 2a$$

$\Downarrow$



$$\sin 30^\circ = \frac{a}{h}$$

$$\frac{1}{2} = \frac{a}{h}$$

$$h = 2a$$

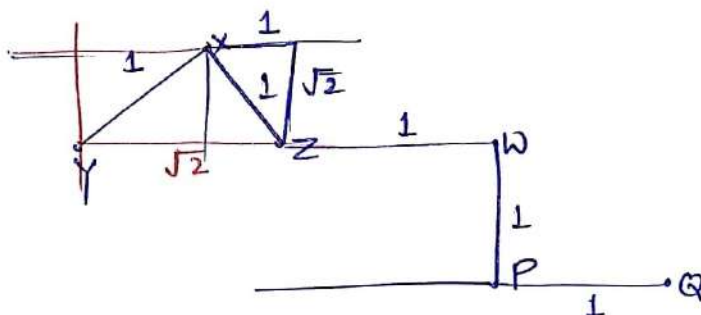
Pg 74

Q 52

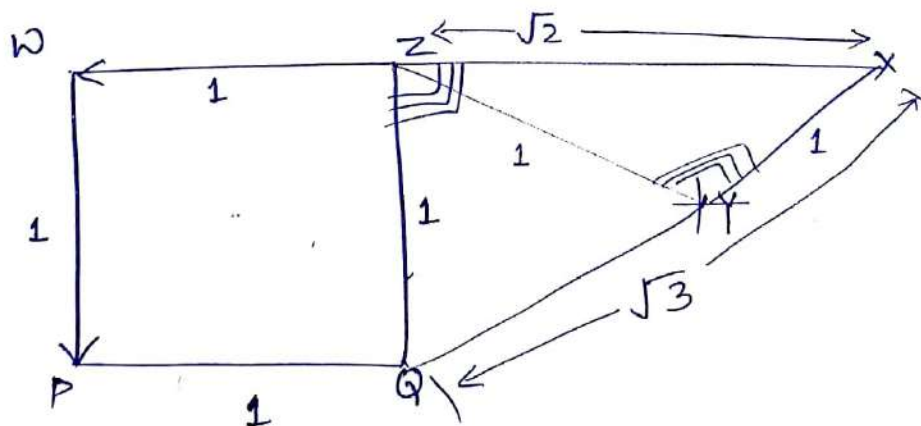
$$+\sqrt{2} + 1 - \cancel{1} + \cancel{1}$$

$$+1 - \sqrt{2} + 1 - \cancel{1} + \cancel{1}$$

2



SIR



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